

Chapter 4
THERMAL SCATTERING DATA

Thermal scattering law data, $S(\alpha,\beta)$ are included for:

H in H ₂ O	8 temperatures from 293.6 to 623.6 K
D in D ₂ O	8 temperatures from 293.6 to 673.6 K
C in graphite	11 temperatures from 293.6 to 3 000 K
Be	8 temperatures from 293.6 to 1 200 K
H in polyethylene	2 temperatures, 293.6 and 350 K

The thermal scattering models are described in JEF Report 2 by J. Keinert and M. Mattes, IKE Stuttgart, "JEF-1 Scattering Law Data" (IKE 6 147, Sept. 1984). New evaluations of the phonon frequency spectra were made for H₂O and D₂O. For graphite and Be the lattice-dynamics model used to derive the phonon frequency spectrum is the same as that used for deriving the ENDF/B-III data.

The $S(\alpha,\beta)$ values are tabulated on a finer α,β mesh than that used for the ENDF/B thermal scattering data current at the time the evaluations were made. Extensive comparisons have been made with experiments.

Pointwise data have also been produced (using a modified version of NJOY-89.62) for the cold moderators, liquid ortho and para hydrogen at 20.38 K and liquid ortho and para deuterium at 23.65 K. Pointwise data have been produced because the corresponding scattering law data, $S(\alpha,\beta)$, have three digit exponents and require to be processed on 64 bit computers.

The $S(\alpha,\beta)$ data are taken from the JEF-1 scattering law data file (or the IKE file in the case of Be) and converted to ENDF-6 format. The number of principal atoms is added, and the principal atom scattering cross-section now agrees with the current general purpose evaluation. The effective temperatures for the principal atom have also been added. The files for H(H₂O,) and D(D₂O) date from November 1990 and those for Be, graphite and polyethylene from July 1991; they were prepared by M. Mattes of IKE Stuttgart.

Thermal scattering law data in the incoherent approximation have been generated using the code GASKET version 2 [5]. A maximum neutron energy transfer of 1.8554 eV was assumed using NMESH = 1 in GASKET-2. If the alpha or beta required is outside the range of the table in File 7, the differential scattering cross-section can be computed with the "short collision time" (SCT) approximation using the corresponding effective scattering temperatures T_{eff} . This is done e.g. in the THERMR module of NJOY [6].

The authors point out that data for intermediate temperatures should be obtained by interpolating between the resulting cross-sections and not by interpolating $S(\alpha,\beta)$.

H(H₂O)

Thermal neutron scattering law data in MF =7 are given for the temperatures:

$$T = 293.6, 323.6, 373.6, 423.6, 473.6, 523.6, 573.6, 623.6 \text{ K}$$

Incoherent scattering (MT = 4) is represented by the thermal neutron scattering law $S(\alpha, \beta, T)$.

The frequency spectrum of hydrogen bound in water (H₂O) is based on a re-evaluation of the scattering dynamic model given in Refs. [1] and [2] at IKE. The improvements are as follows (Ref. [7]):

- Temperature dependence for the translational mass of H₂O is based on the results of Eucken [3].
- Temperature dependence for the hindered rotational band derived from Haywood and Page [4].
- -The two discrete vibrational modes for the intramolecular oscillations remained unchanged.

With this frequency distribution, thermal scattering law data have been generated for one hydrogen atom in the H₂O molecule in incoherent approximation using the code GASKET-2.

D(D₂O)

Thermal neutron scattering law data in MF = 7 are given for the temperatures:

$$T = 293.6, 323.6, 373.6, 423.6, 473.6, 523.6, 573.6, 673.6 \text{ K}$$

Incoherent scattering (MT = 4) is represented by the thermal neutron scattering law $S(\alpha, \beta, T)$.

The frequency spectrum of deuterium bound in heavy water (D₂O) is based on a re-evaluation of the scattering dynamic model given in [8,9]. The modifications are as follows:

- Upper oscillator frequency increased to 0.338 eV, being consistent with the value for H in H₂O.
- Re-normalisation of the temperature dependent band of hindered rotations derived from the results of Haywood and Page [10].
- Translational mass unit = 20.0 (temperature independent).

With this frequency distribution thermal scattering law data have been generated for one deuterium atom in the D₂O molecule in incoherent approximation with the code GASKET-2.

Beryllium

Thermal neutron scattering law data in MF = 7 are given for the temperatures:

$$T = 293.6, 400, 500, 600, 700, 800, 1\ 000, 1\ 200 \text{ K}$$

- Coherent elastic scattering (MT = 2): The quantity actually given in the file is $S(E,T)$, which is conveniently represented as a stair-step function with breaks at the Bragg edges using histogram interpolation. Bragg edges and structure factors are derived from the cross-section.
- Incoherent inelastic scattering (MT = 4) is represented by the thermal neutron scattering law $S(\alpha,\beta,T)$.

The frequency spectrum of polycrystalline beryllium was derived from a central force lattice dynamical model calculation of the unit cell [11,12]. With this frequency distribution the thermal scattering law data have been generated in incoherent approximation with the code GASKET-2.

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Thermal neutron scattering law data in MF = 7 are given for the temperatures:

$$T = 293.6, 400, 500, 600, 700, 800, 1\ 000, 1\ 200, 1\ 600, 2\ 000, 3\ 000\ \text{K}$$

- Coherent elastic scattering (MT = 2): The quantity actually given in the file is $S(E,T)$, which is conveniently represented as a stair-step function with breaks at the Bragg edges using histogram interpolation. Bragg edges and structure factors are derived from the cross-section.
- Incoherent inelastic scattering (MT = 4) is represented by the thermal neutron scattering law $S(\alpha,\beta,T)$.

The frequency spectrum for carbon bound in graphite was derived from a central force lattice dynamical model calculation of the graphite unit cell [12,13]. With this frequency distribution the thermal scattering law data have been generated in incoherent approximation with the code GASKET-2.

H in polyethylene

Thermal neutron scattering law data in MF = 7 are given for the temperatures $T = 293.6$ and $350\ \text{K}$.

- Incoherent elastic scattering (MT = 2) is represented using a bound cross-section and Debye-Waller integral given in the file as $W'(T)$ divided by the atomic mass (1/eV) as a function of temperature (K).
- Incoherent inelastic scattering (MT = 4) is represented by the thermal neutron scattering law $S(\alpha,\beta,T)$.

The phonon frequency spectrum of hydrogen bound in polyethylene was derived by Sprevak and Koppel [14] in calculating the dispersion relations for the infinite chain of CH_2 radicals as well as the polarisation vector for each normal frequency using the set of force constants determined by Lin and Koenig [15]. The weighted frequency spectrum was then calculated using the computed dispersion relations and the computed amplitude vectors.

The $S(\alpha,\beta)$ data are generated for one hydrogen atom in the CH_2 molecule in incoherent approximation for two temperatures with the code GASKET-2.

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