



**UNIVERSITY OF CALIFORNIA AT
BERKELEY**

NUCLEAR ENGINEERING DEPARTMENT

TRANSMUTATION CAPABILITY OF MOLTEN SALT REACTORS FUELED WITH TRU FROM LWR

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MSR Features

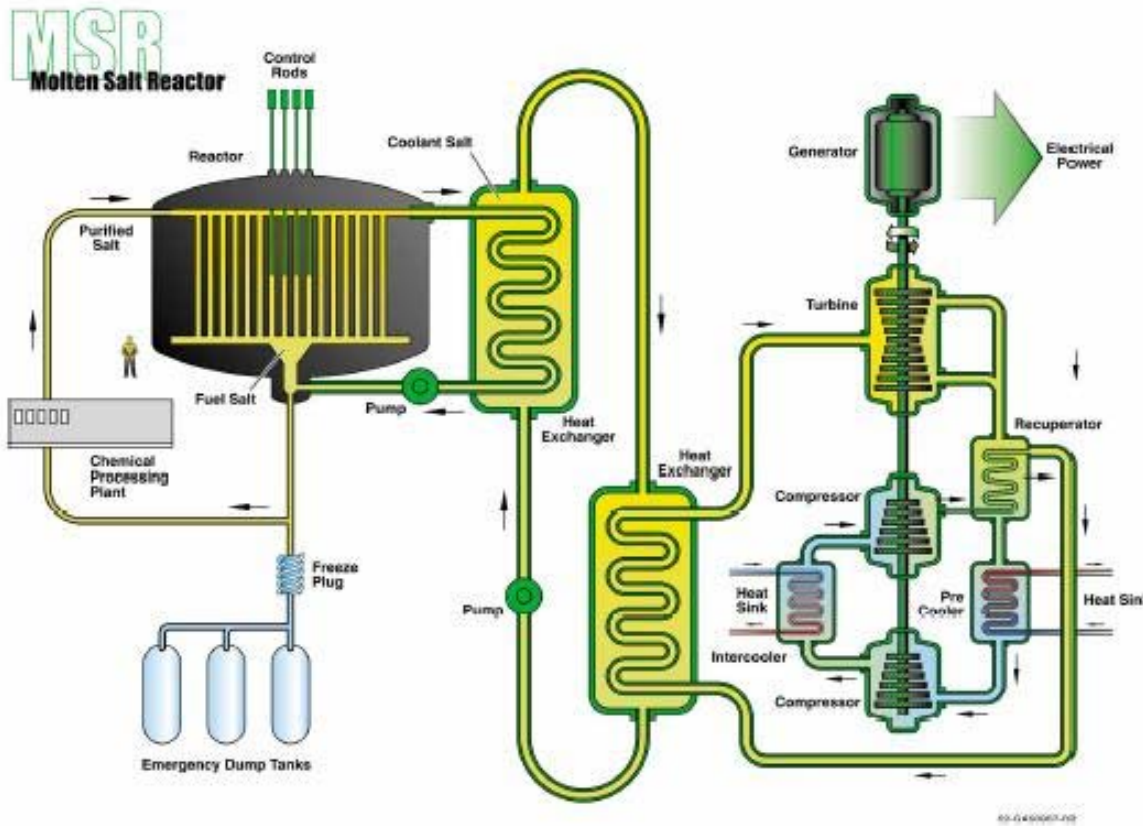
$\text{NaF} - \text{ZrF}_4 - \text{AcF}_3$

$600 \div 700 \text{ }^\circ\text{C}$

Once-through

*Suggested by
Charles Bowman*

*Fed by TRU from
spent fuel from
LWR after a burnup
of $33 \text{ GWD/t}_{\text{HM}}$ and
10 years of cooling
and after U
isotopes extraction*



Objectives

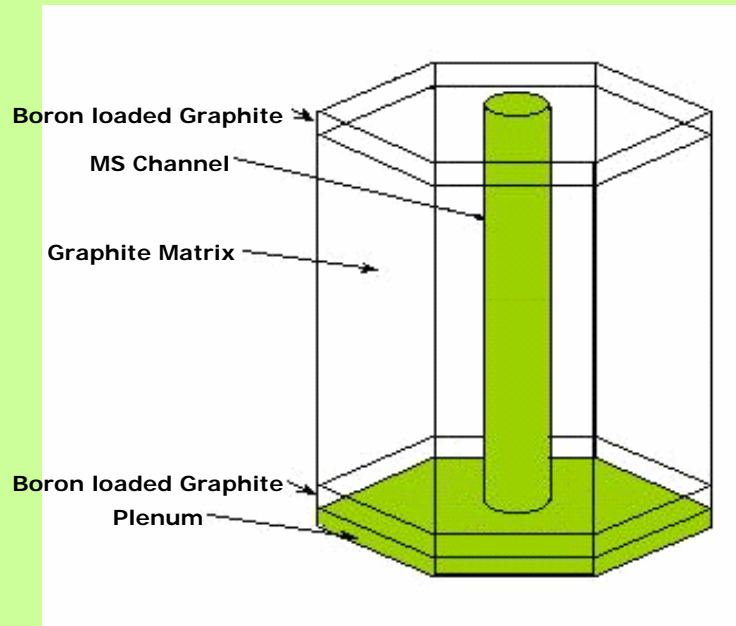
- 1. Assess the feasibility of attaining criticality in a finite core*
- 2. Evaluate MSR performance sensitivity to design variables*
- 3. Evaluate repository implications*
- 4. Compare transmutation efficiency for different TRU burner systems*

Previous work

Graphite-to-MS volume ratio
(C/MS) = 3

$D_{channel} = 7 \text{ cm}$, $H = 420 \text{ cm}$

$k_{eff} = 1.032$ (with axial leakage)



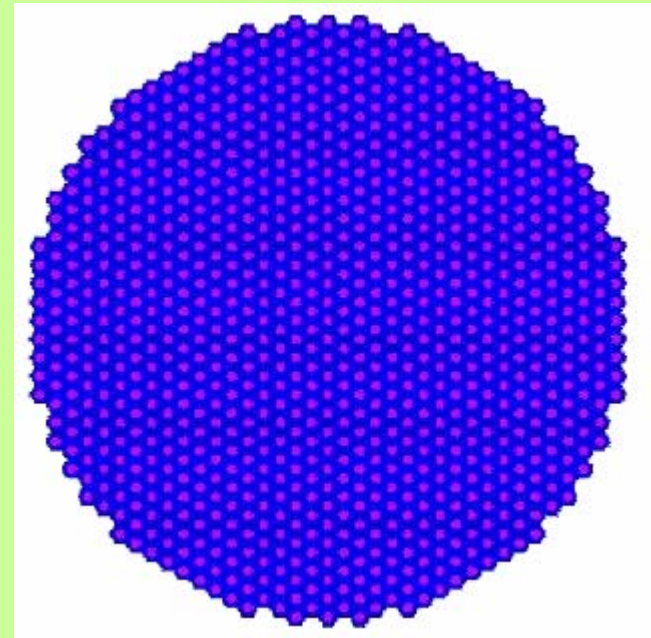
1. Finite Model

$H/D_{core} = 0.924$, 955 channels

5733 MW_{th} (390 W/cm^3)

$k_{eff} = 1.00247$ (± 0.00067)

MCNP4C

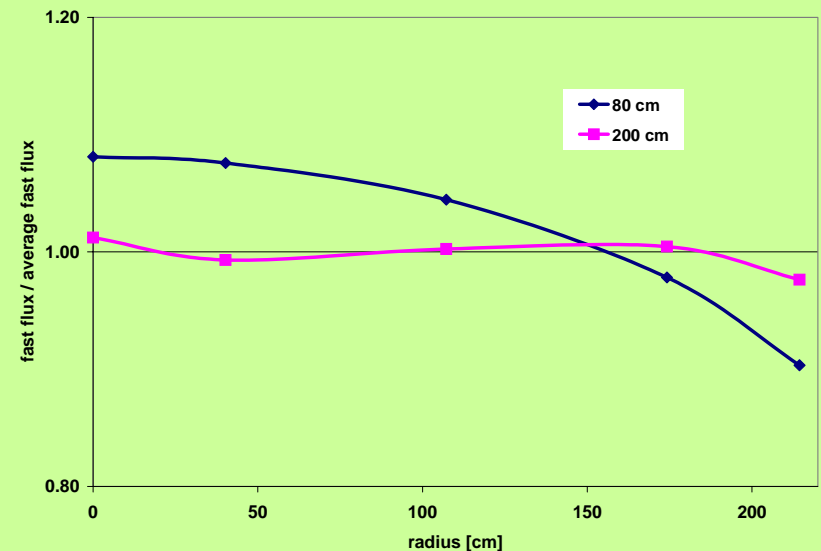
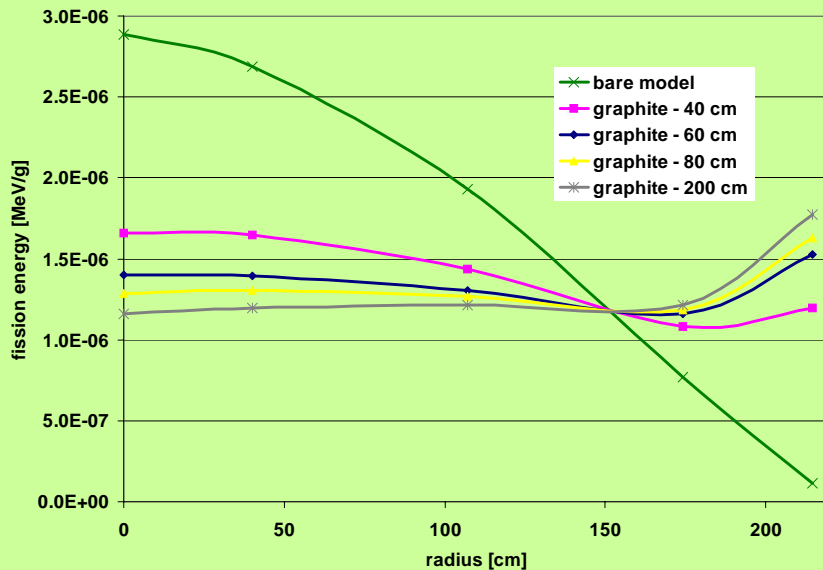


1. Radial Reflector

Graphite Thickness [cm]	k_{eff}	Radial Leakage Probability
0	1.00247 (± 0.00067)	2.56 %
40	1.01916 (± 0.00059)	2.74 %
60	1.02574 (± 0.00059)	2.85 %
80	1.02848 (± 0.00058)	2.78 %
200	1.03088 (± 0.00059)	2.79 %

(Due to statistics)

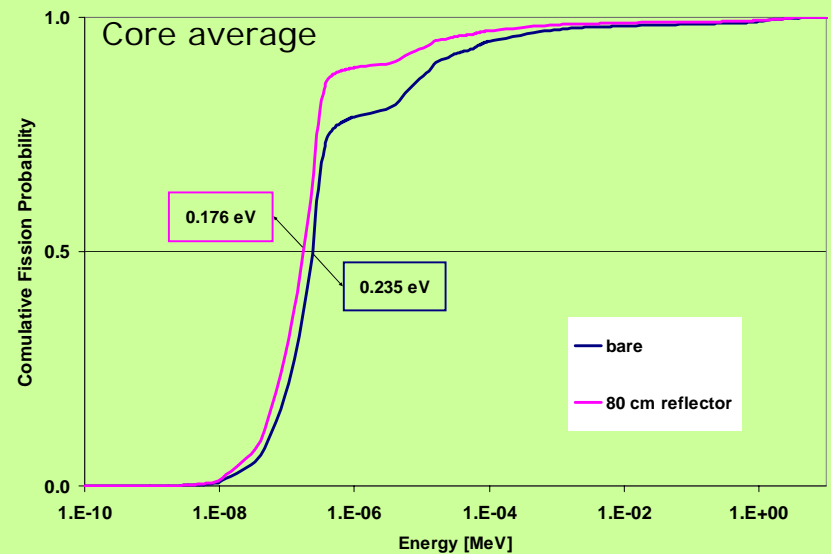
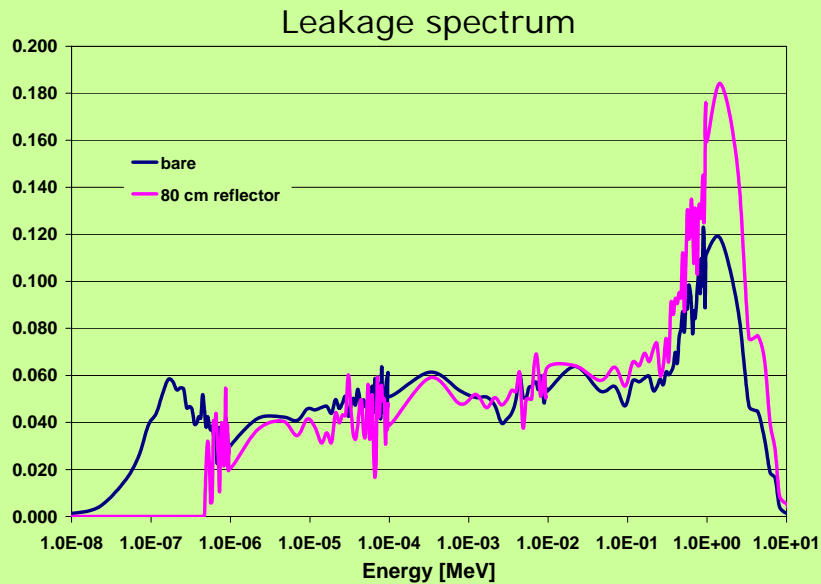
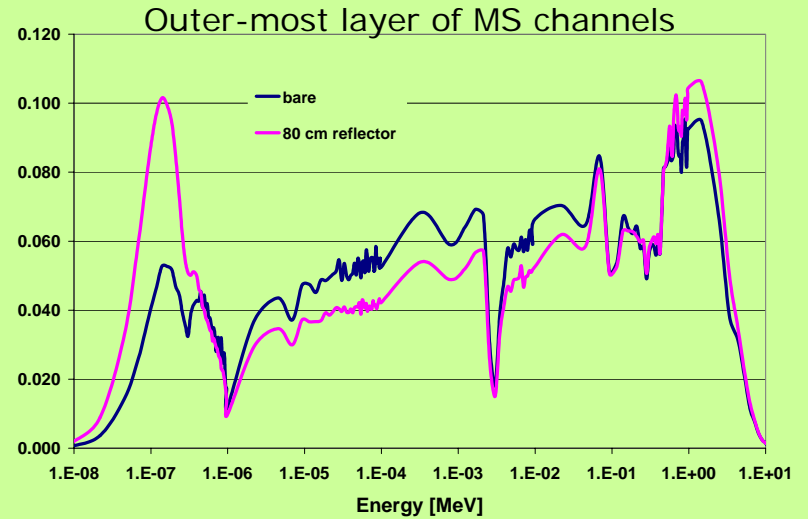
Limit:
Maximum fast neutrons fluence (> 0.01 MeV) in the graphite
 $3 \cdot 10^{22}$ neutrons/cm²



1. Leakage Probability

Graphite double effect:

- . reflector*
- . moderator*

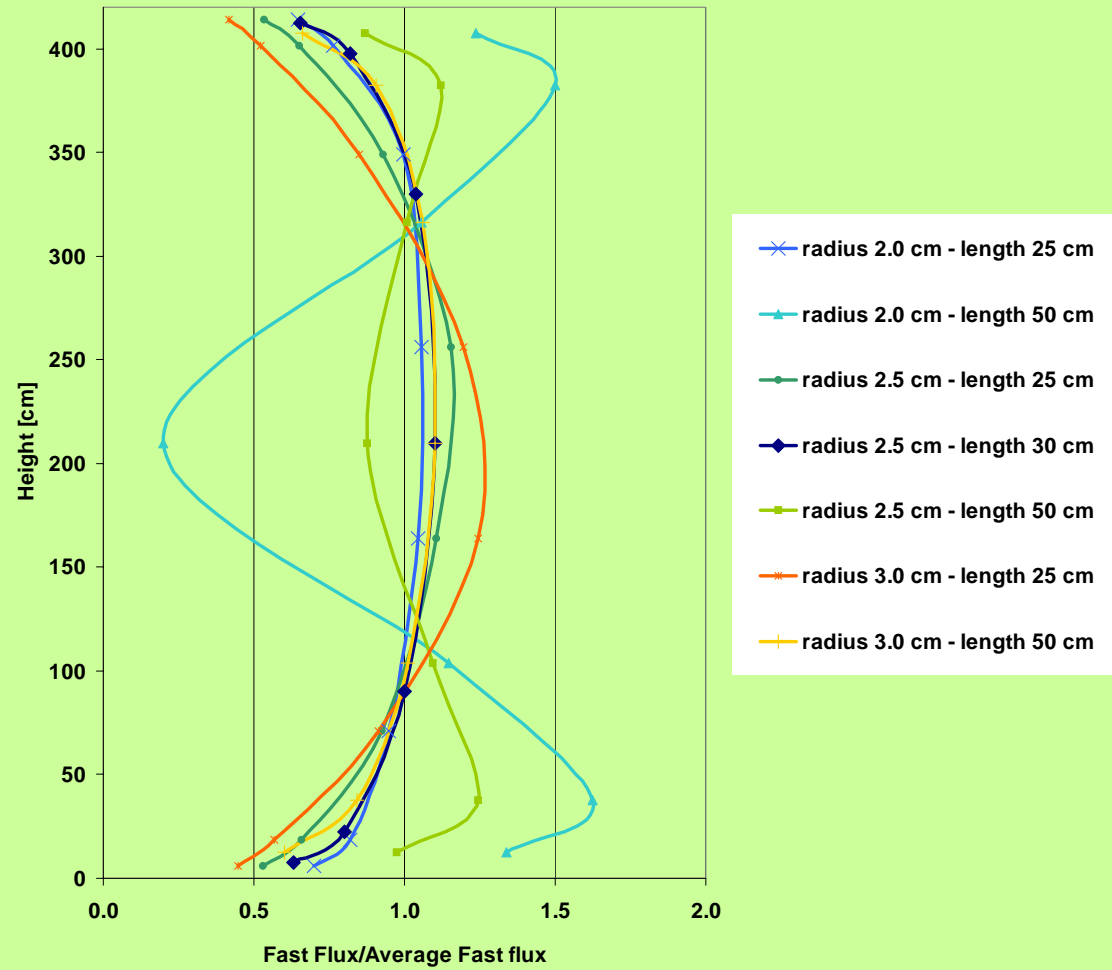


1. Axial Reflector

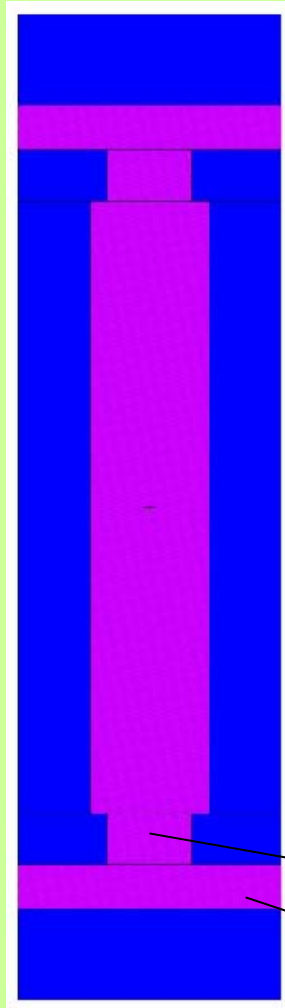
*Problem:
plenum (27 cm) to collect
the salt below and above
the core*

*Graphite beyond plenum
is ineffective reflector*

*Solution: to narrow the
channels diameter at the
extremities*



1. Final Design



*Maximum-to-average fast flux in the graphite **1.079***

$$k_{eff} = 1.04047$$

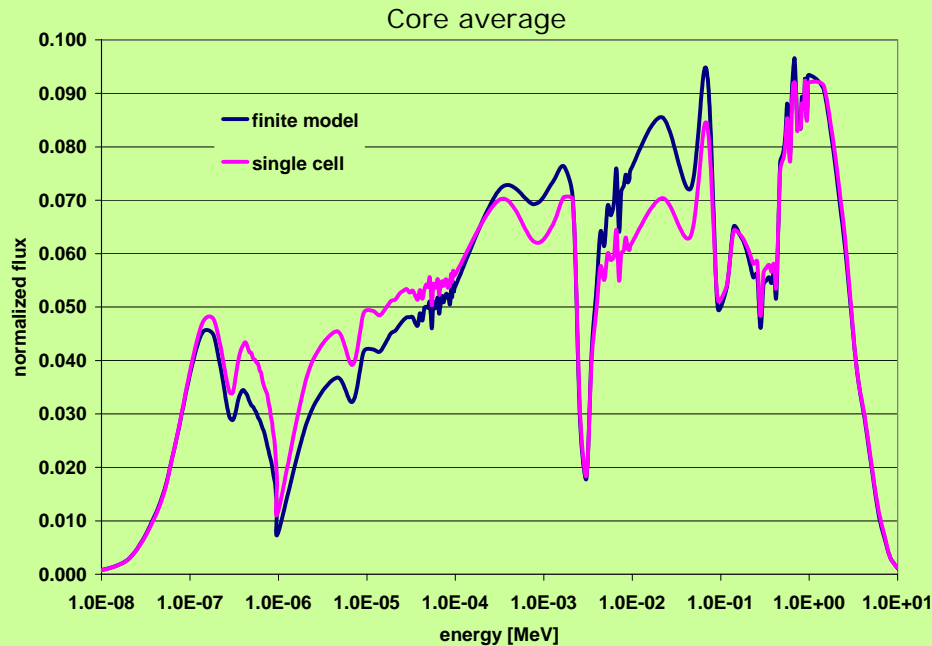
The reactivity excess should compensate for:

- 1. neutrons absorption by fission products*
- 2. fraction of delayed neutrons released out of core*

radius 2.5 cm, length 30 cm

plenum, height 27 cm

1. Equilibrium Composition



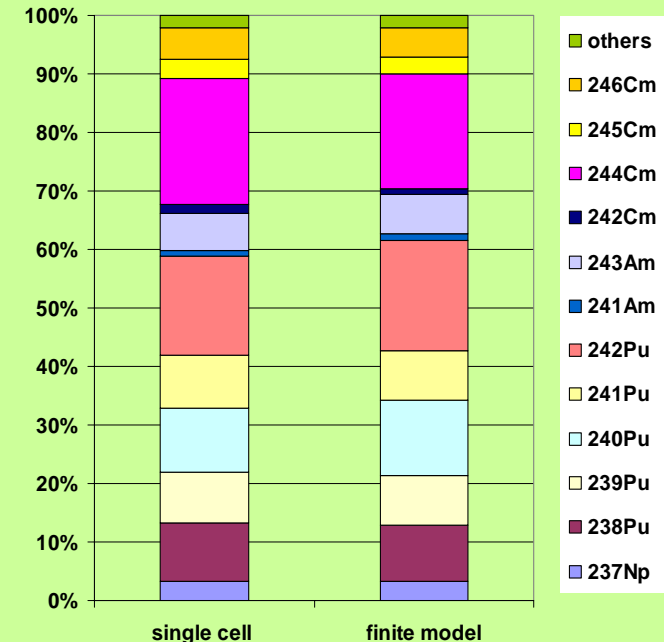
Single cell k_{eff} (updated) = 1.02351

Finite model k_{eff} = 0.98517

- radial leakage (2.53 %)
- increased absorption in non-actinides salt components

C/MS	2.8	3.0	3.2	3.4
k_{eff}	0.98267	0.98517	0.98910	0.98799

∴ Finite core can not be critical with NaF-ZrF₄ even if fission products are extracted immediately



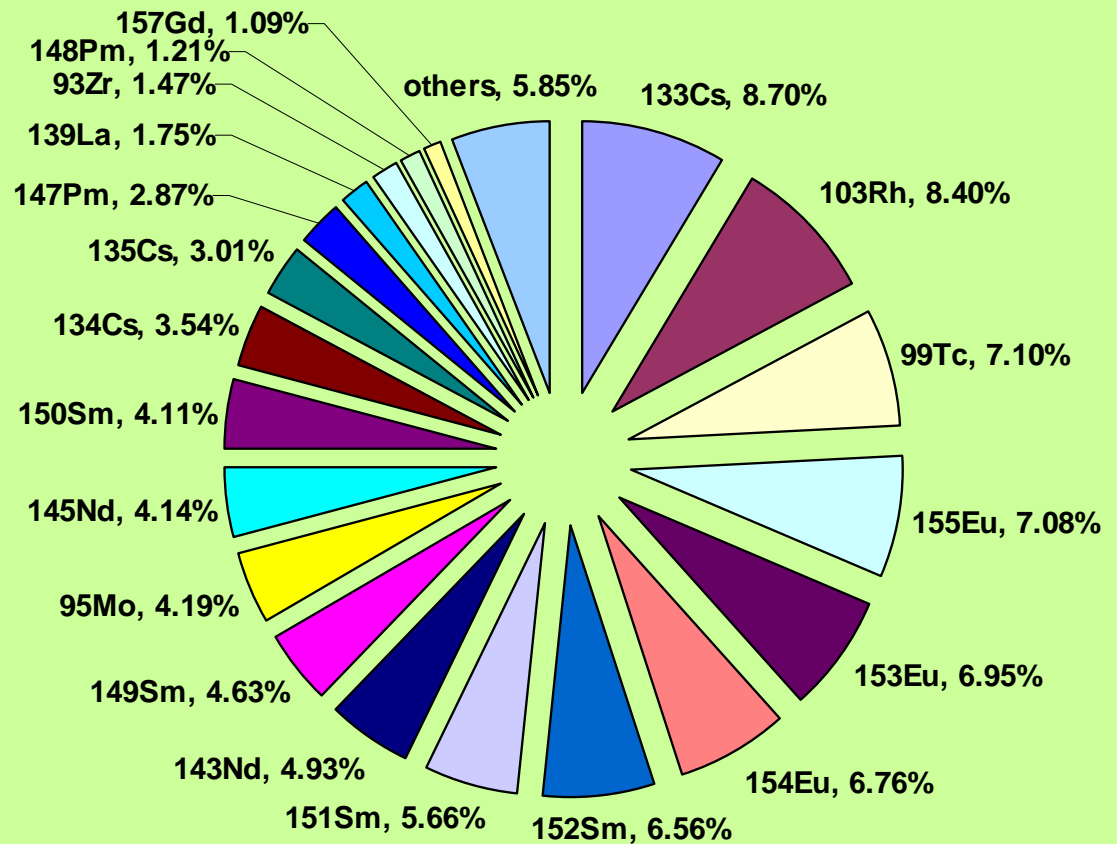
Equilibrium composition

1. Fission Products ρ Effect

No Extraction

If FP are not removed
at all, $\Delta k_{\text{eff}} = -0.222$

Not manageable



Fractional absorption by FP

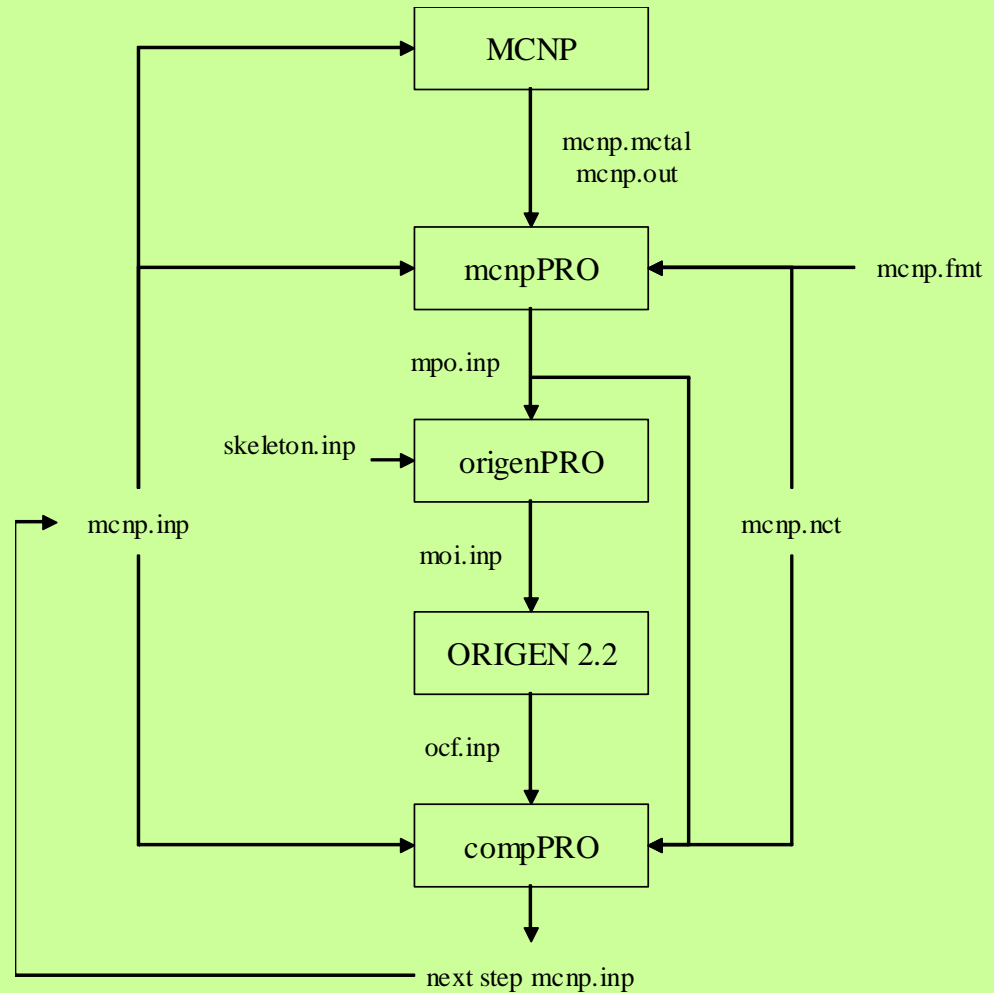
1. Fission Products ρ Effect

Fission products residence time

FP	Residence Time
Kr, Xe	50 s
Nb, Mo, Ru, Rh, Tc	2.4 h
La, Ce, Pr, Nd, Pm, Sm, Eu	< 50.4 d
Y	1 y
Sr, Ba, Cs	Salt residence time

$$\Delta k_{eff} = -0.018$$

Manageable!



2. Sensitivity Analysis

Design variables:

- 1. C/MS (spectrum)*
- 2. Feed Rate*
- 3. Power Density*

Performance parameters considered:

- 1. K_{eff} (finite unit cell)*
- 2. Graphite lifetime*
- 3. Transmutation Efficiency*

$$FT = \frac{\sum_i N_{i,feed} - \sum_i N_{i,equilibrium}}{\sum_i N_{i,feed}}$$

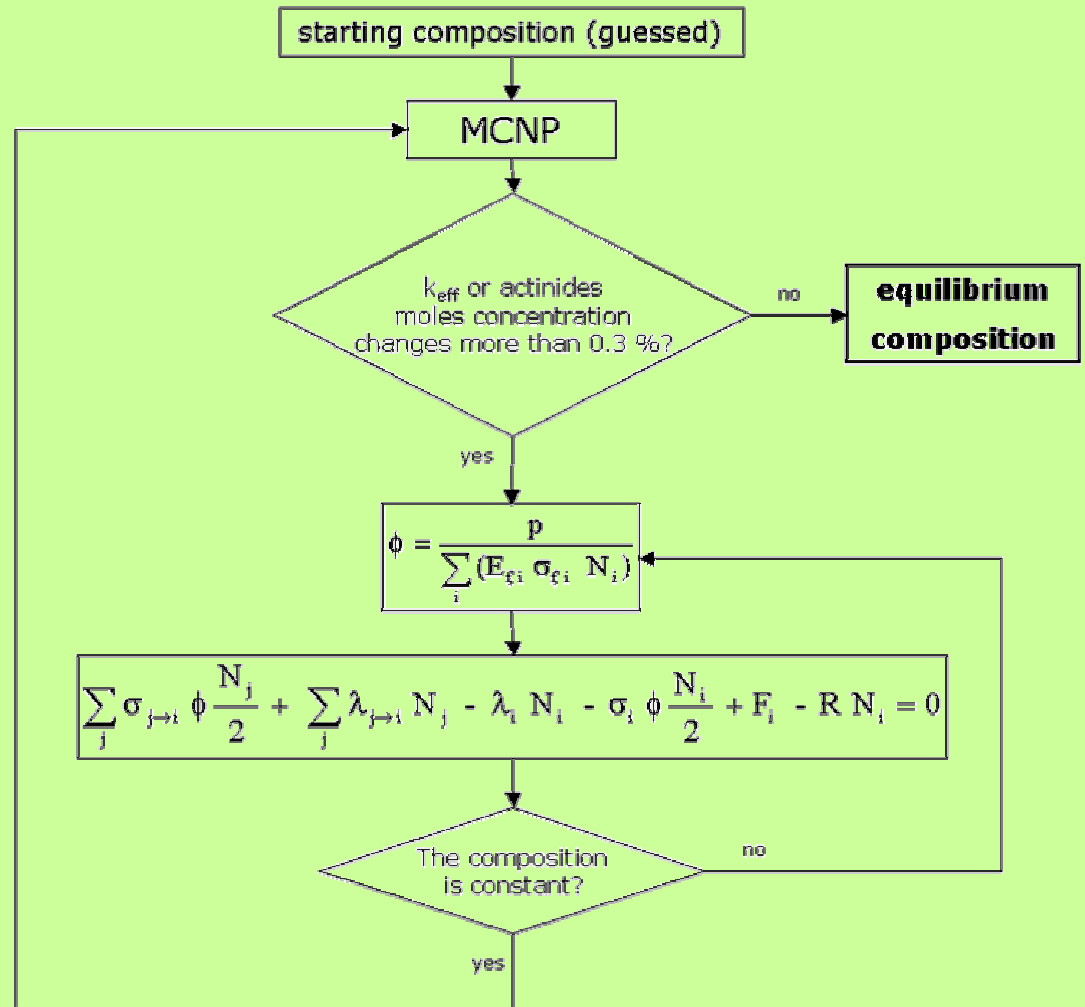
2. Eq. Composition Determination

34 actinides

reaction: fission, (n, γ) ,
 $(n, 2n)$, $(n, 3n)$

Constraints:

- Actinide fluorides maximum solubility in the salt **1.56 mol%**
- maximum fast neutrons fluence (> 0.01 MeV) in the graphite **$3 \cdot 10^{22}$ neutrons/cm²**



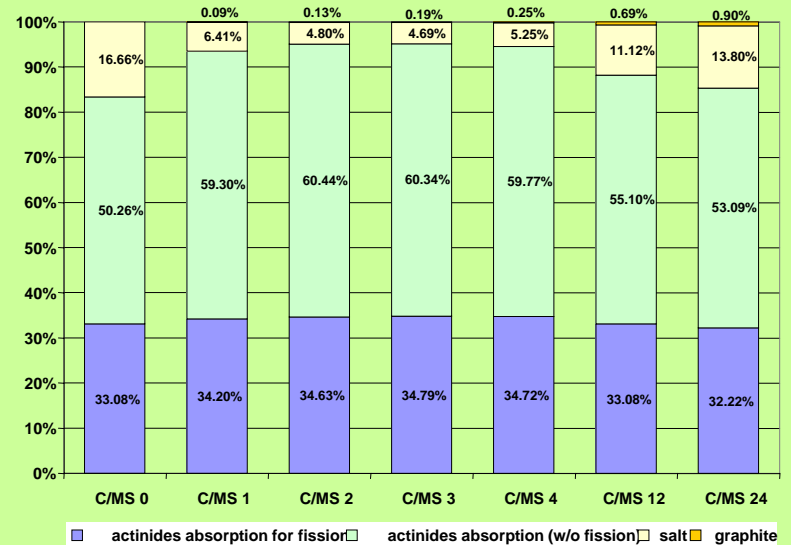
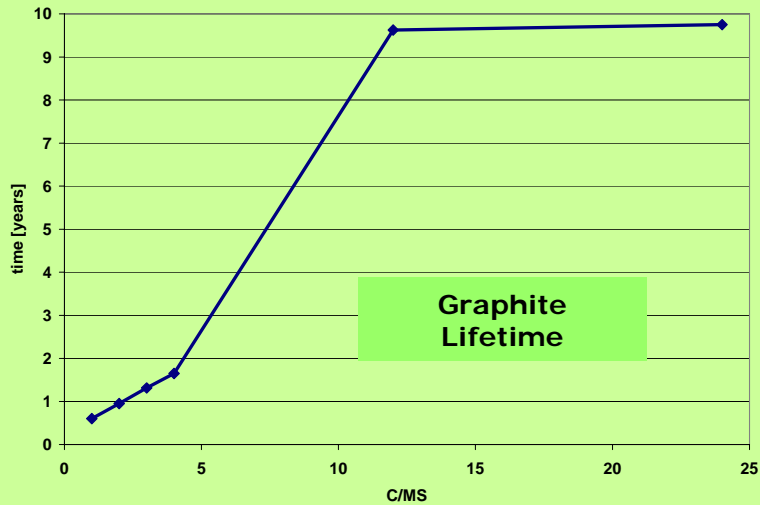
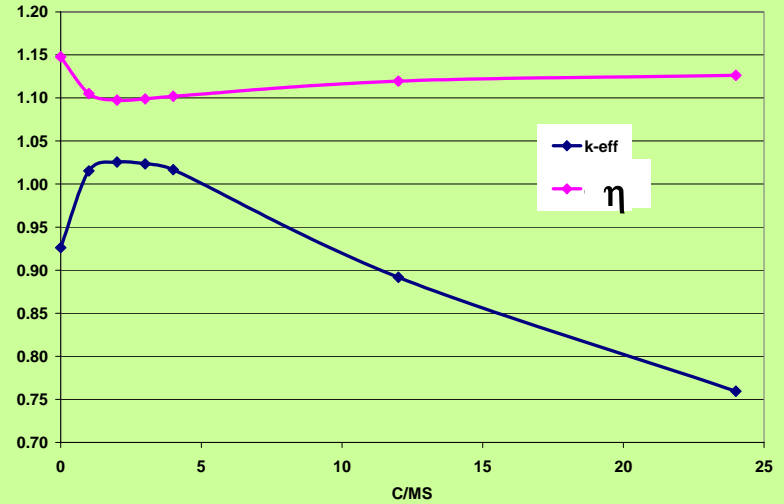
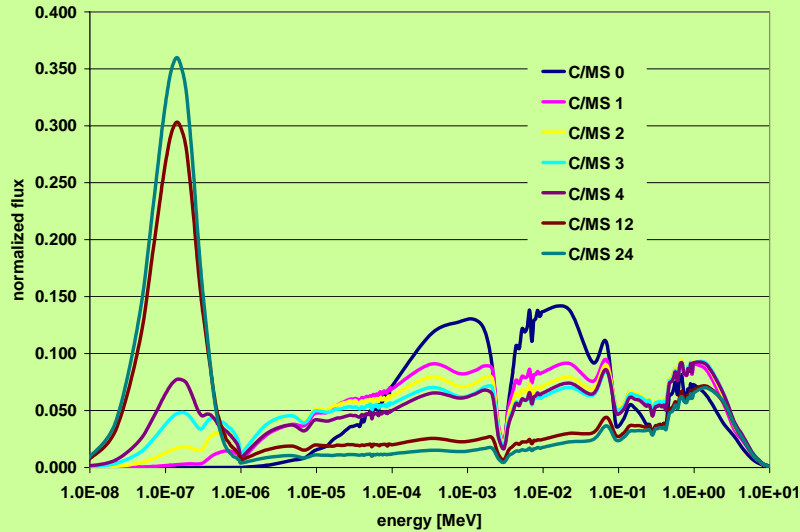
2. Feed Rate Effect

C/MS=3, power density=390 W/cm³

Characteristics	MS Feed Rate [I/day-GW _{th}]			
	0.133	0.267	0.533	1.067
k_{eff}	1.01869	1.01760	1.02031	1.02351
Graphite Lifetime [years]	1.371	1.371	1.374	1.379
MS Residence Time [years]	105	53	26	13
Transmutation Efficiency	98.6%	97.2%	94.5%	89.6%

The transmutation efficiency strongly depends on MS feed/extraction rate

2. Spectrum Effect

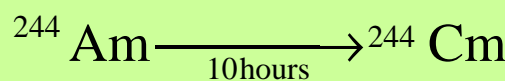
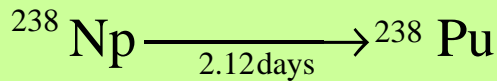


2. Power Density Effect

C/MS=3, power density=39 W/cm³

Characteristics	Feed Rate [l/day-GW _{th}]			
	0.133	0.267	0.533	1.067
K_{eff}	0.95481	0.95443	0.95514	0.96159
<i>[vs k_{eff} for 390 W/cm³]</i>	<i>1.01869</i>	<i>1.01760</i>	<i>1.02031</i>	<i>1.02351</i>
Graphite Lifetime [years]	13.881	13.882	13.887	13.908
Transmutation Efficiency	98.55%	97.15%	94.37%	89.47%

$$\sum_j \sigma_{j \rightarrow i} \frac{\phi}{2} N_j + \sum_j \lambda_{j \rightarrow i} N_j - \lambda_i N_i - \sigma_i \frac{\phi}{2} N_i + F_i - R N_i = 0$$



Actinide	Cross Section [barns]	
	Capture	Fission
²³⁸ Np	11	105
²³⁸ Pu	21	2
²⁴⁴ Am	36	150
²⁴⁴ Cm	18	0.6

3. Waste

Radio-toxicity

defines radiation related hazard

Decay Heat

defines the concentration limit of actinides in the repository

^{237}Np and precursors

long term radiation hazard due to leakage out of repository

Fissile Pu

Proliferation hazard

*Methodology:
Exponential
Matrix to
follow decay*

$$\frac{dN_i(t)}{dt} = \sum_j \lambda_{j \rightarrow i} N_j(t) - \lambda_i N_i(t)$$

$$\frac{d\vec{N}(t)}{dt} = A\vec{N}(t)$$

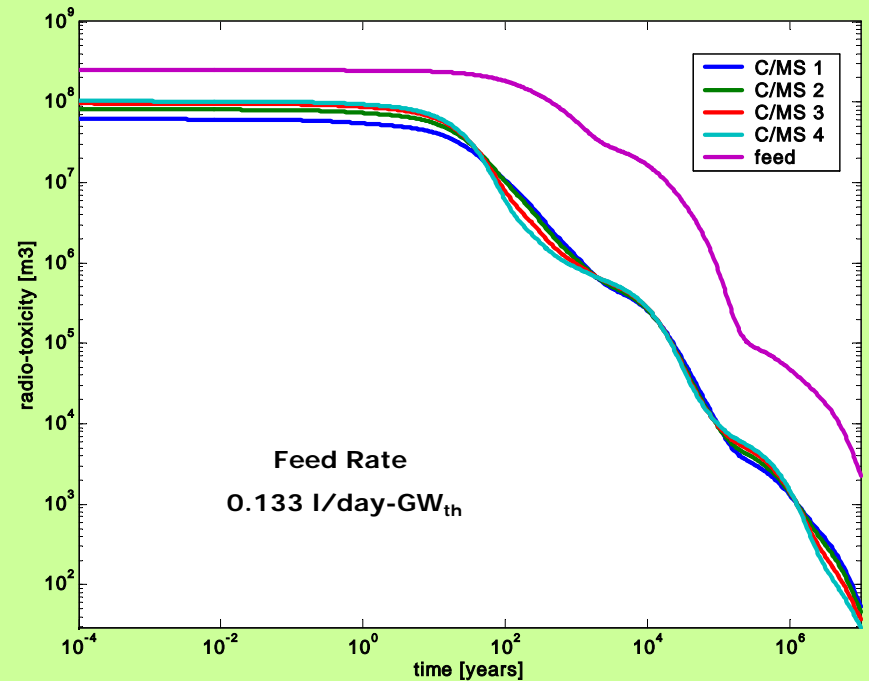
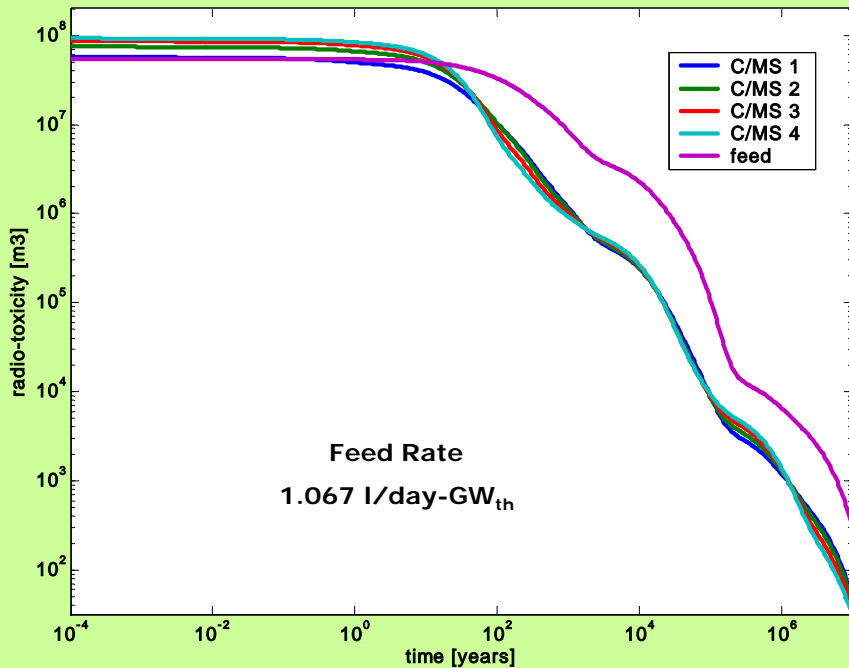
$$\vec{N}(t) = \vec{N}_{t=0} e^{At}$$

3. Radio-toxicity

Ingestion Toxicity Index

the volume of water with which the mixture of radio nuclides must be diluted so that drinking the water will result in accumulation of radiation dose at a rate no greater than 0.5 rem/year

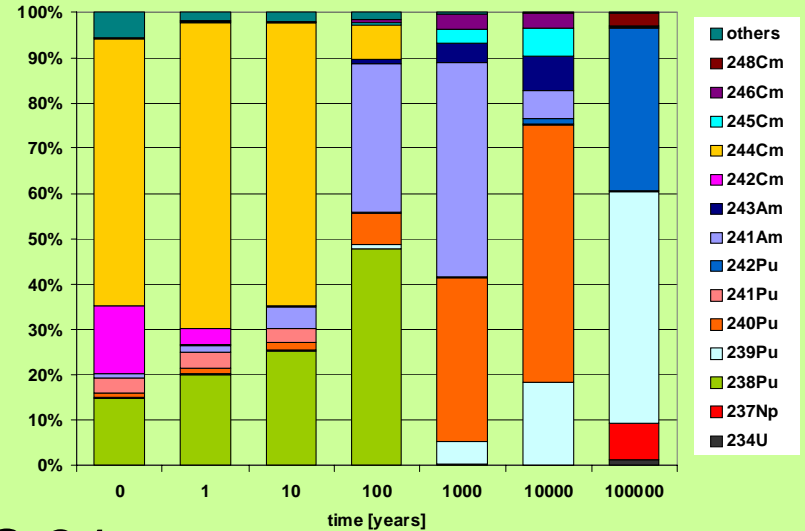
$$TI = \sum_i \frac{\lambda_i N_i}{C_i}$$



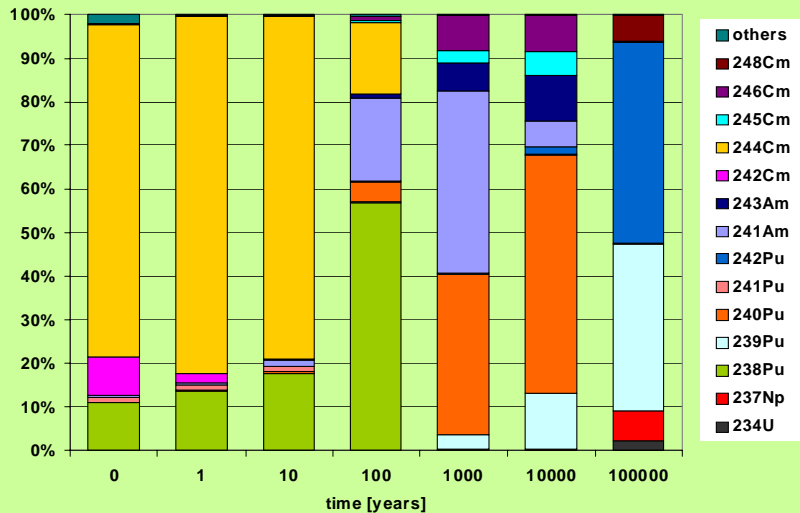
3. Radio-toxicity

Fractional Contribution to radio-toxicity

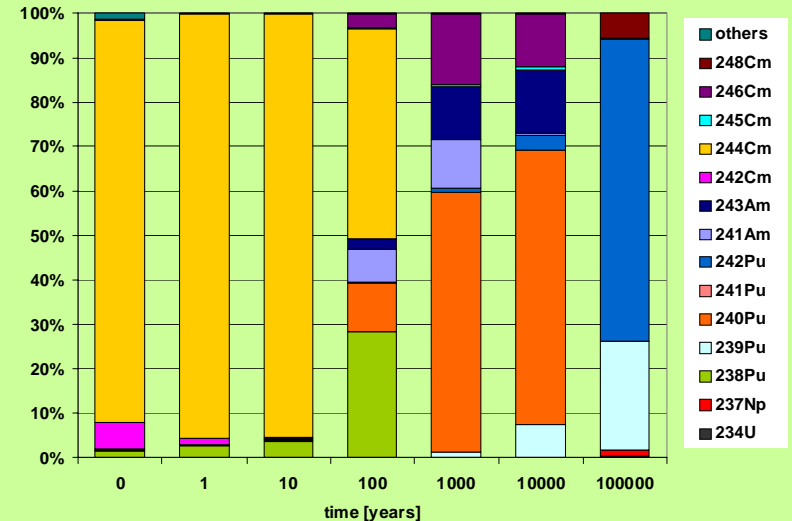
C/MS 0



C/MS 3



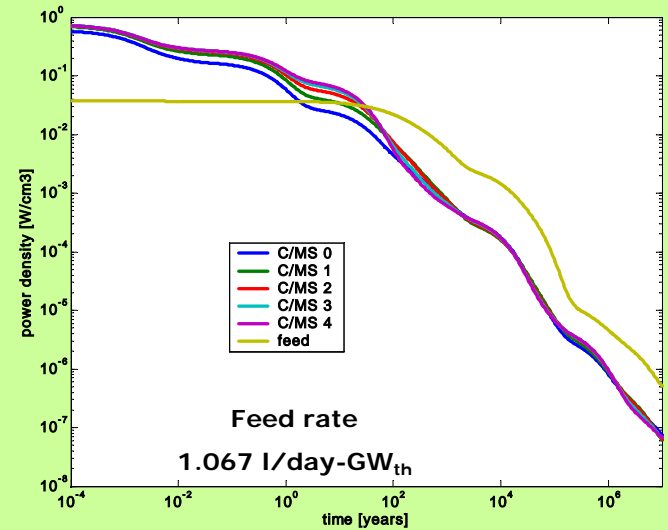
C/MS 24



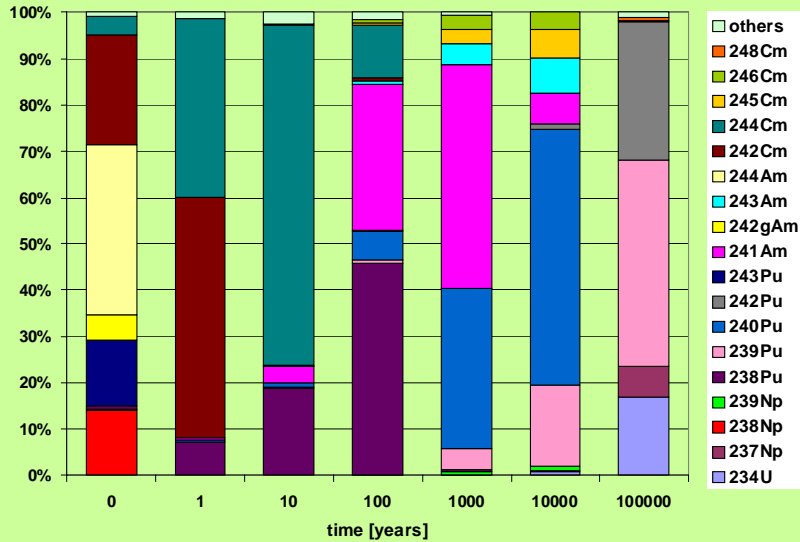
3. Decay Heat

Power Density
[W/cm³ salt]

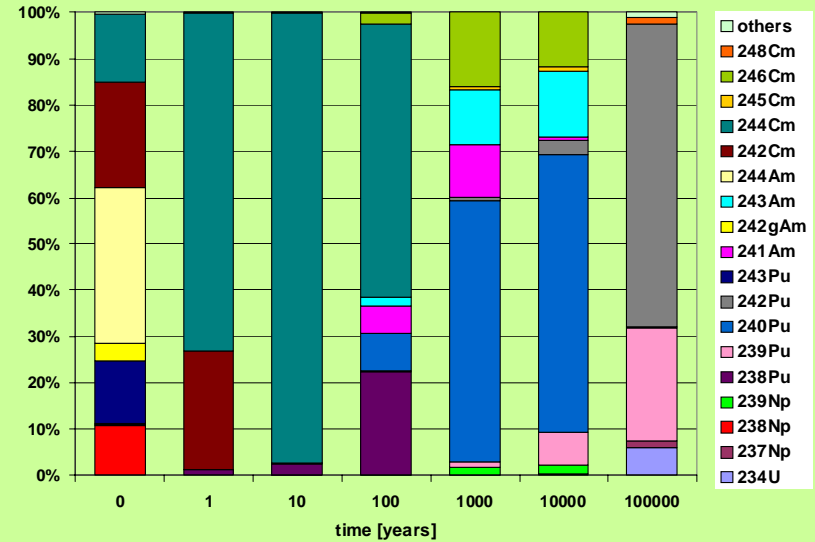
$$p = \sum_i E_i \lambda_i N_i$$



C/MS 0

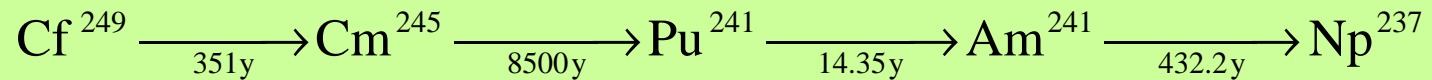


C/MS 24



3. ^{237}Np & Pu

^{237}Np ($T_{1/2}$ $2.144 \cdot 10^6$ years) and precursors:



	Feed	C/MS = 0	C/MS = 3	C/MS = 24
^{237}Np and precursors	1.0	0.105	0.090	0.024
FT ^{239}Pu	-	96.64 %	98.21 %	99.65 %
FT ^{241}Pu	-	83.49 %	87.19 %	97.46 %
$(^{239}\text{Pu} + ^{241}\text{Pu})/\text{Pu}$	64.46 %	35.42 %	28.87 %	7.14 %

Softer spectrum is preferred

4. Systems Comparison

Objective: Compare the transmutation effectiveness dependence on transmuted reactor spectrum

Model: Unit cell continuously fed with TRU from LWR SF and TRU is continuously removed to establish equilibrium concentration

Constraints: - same total fractional transmutation within the same residence time
- fuel dimensions and linear heat rate (power density) as of reference reactor

Systems:

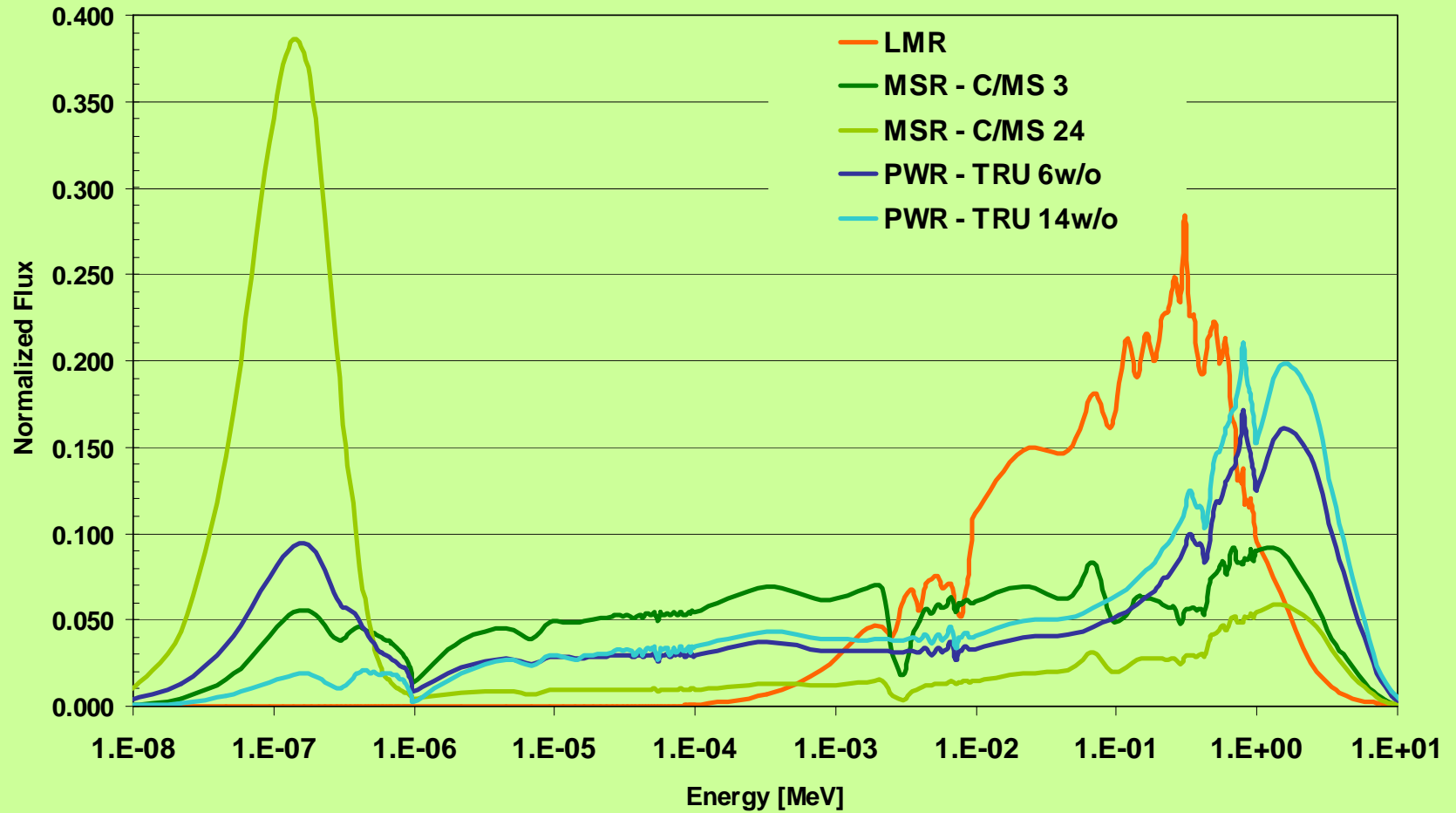
1. Liquid Metal Reactor, Pb-Bi cooled (TRU/Zr fuel)
2. MSR with epithermal spectrum (TRU fluorides)
3. MSR with thermal spectrum (TRU fluorides)
4. PWR with hard spectrum (TRU oxide – 14w/o + ZrO₂)
5. PWR with soft spectrum (TRU oxide – 6w/o + ZrO₂)

4. Reactors Characteristics

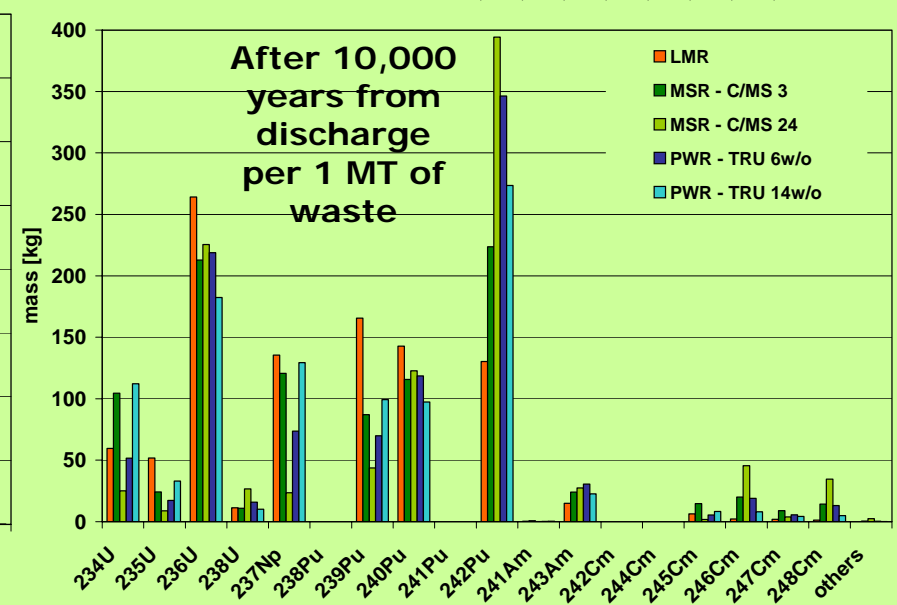
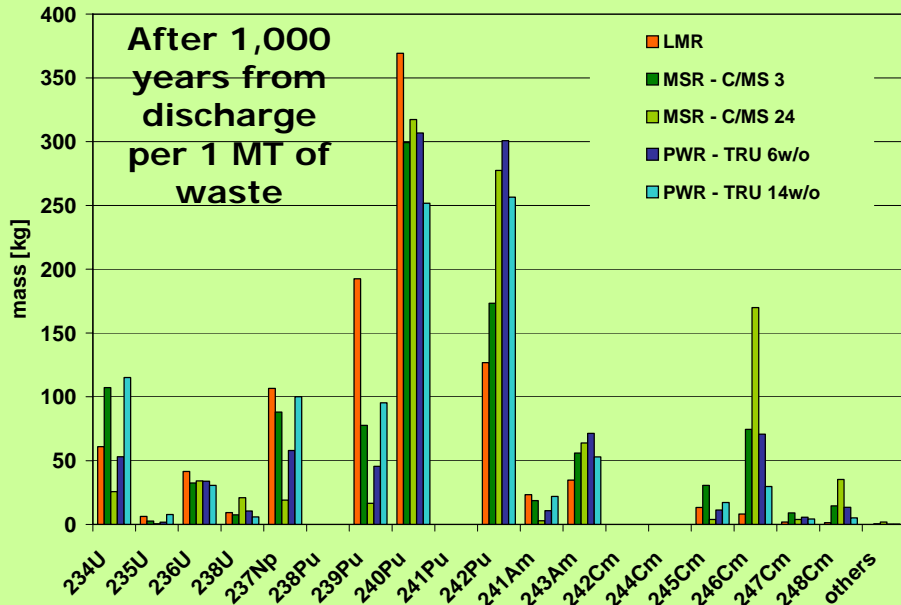
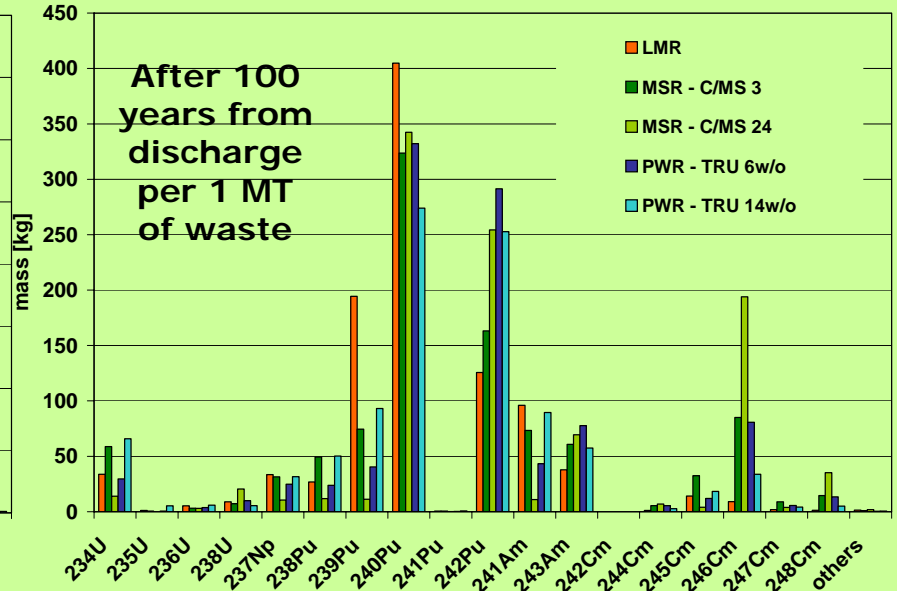
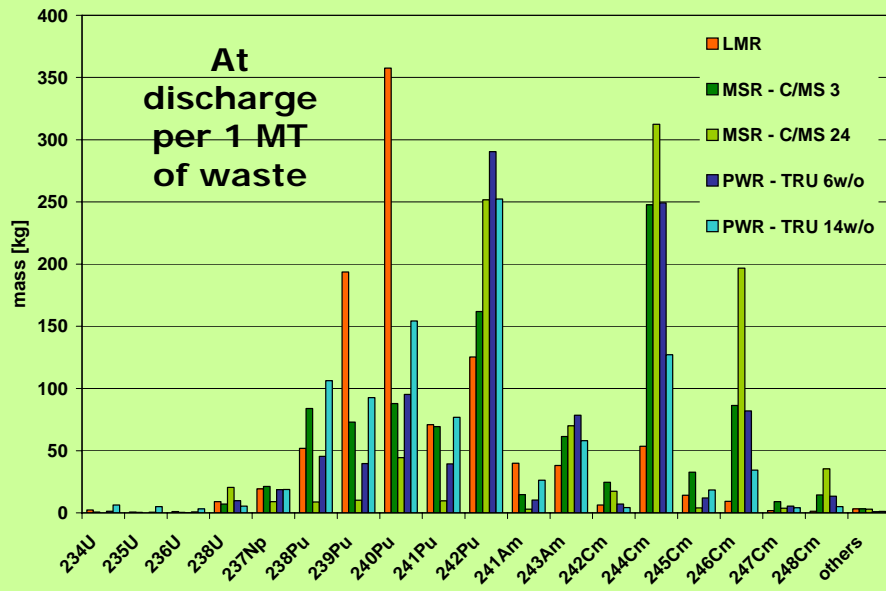
Characteristic	LMR	MSR C/MS 3	MSR C/MS 24	PWR TRU 6 w/o	PWR TRU 14 w/o
k_{eff} (equilibrium)	1.039	1.009	0.670	0.962	1.025
Fast flux [n/cm ² -s]	1.08×10^{16}	2.04×10^{15}	1.63×10^{15}	5.59×10^{14}	4.41×10^{14}
Power density [W/cc] *	181.7	97.50	15.60	110.19	110.19
Specific power [W/g]	766	3435	3403	821	329
Total FT*	99.53%	99.53%	99.53%	99.53%	99.53%
Actinides in core at equil. [atoms/cm ³]	5.94×10^{20}	2.82×10^{20}	2.84×10^{20}	1.00×10^{21}	2.52×10^{21}

* imposed

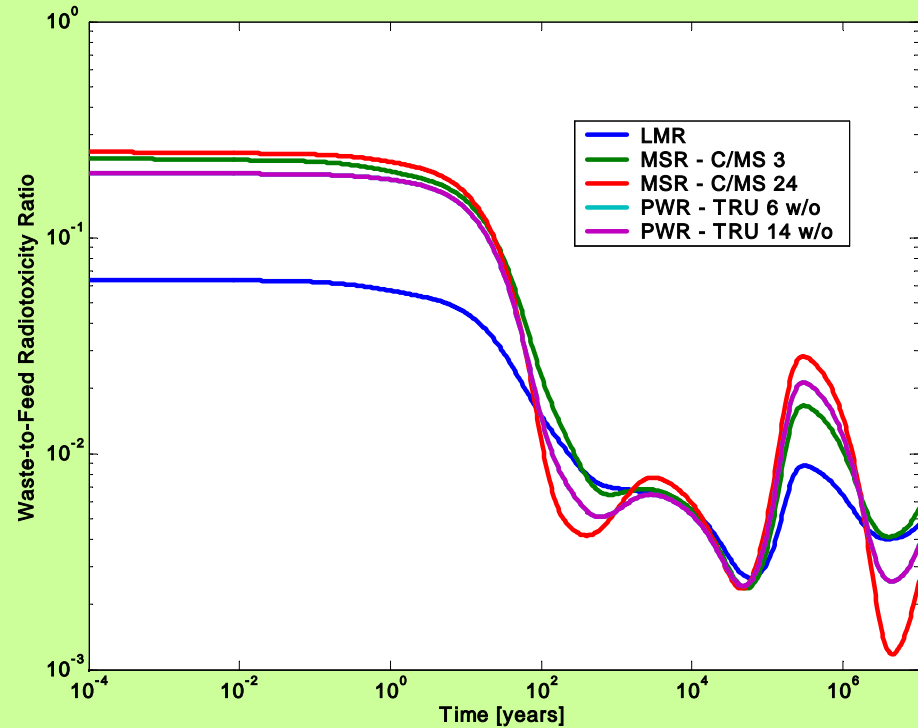
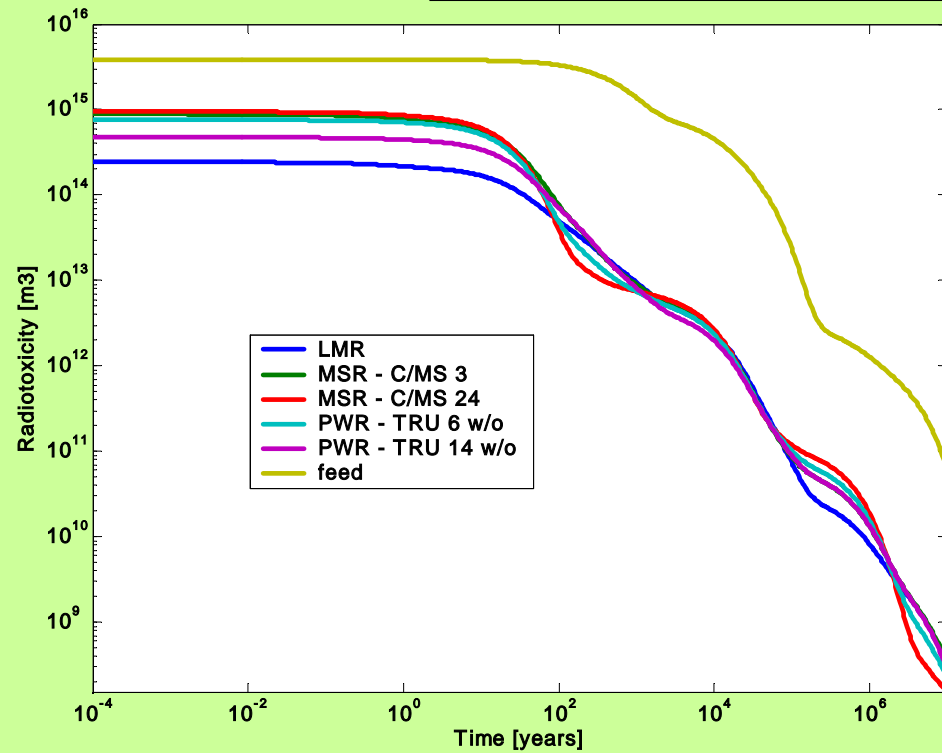
4. Spectra



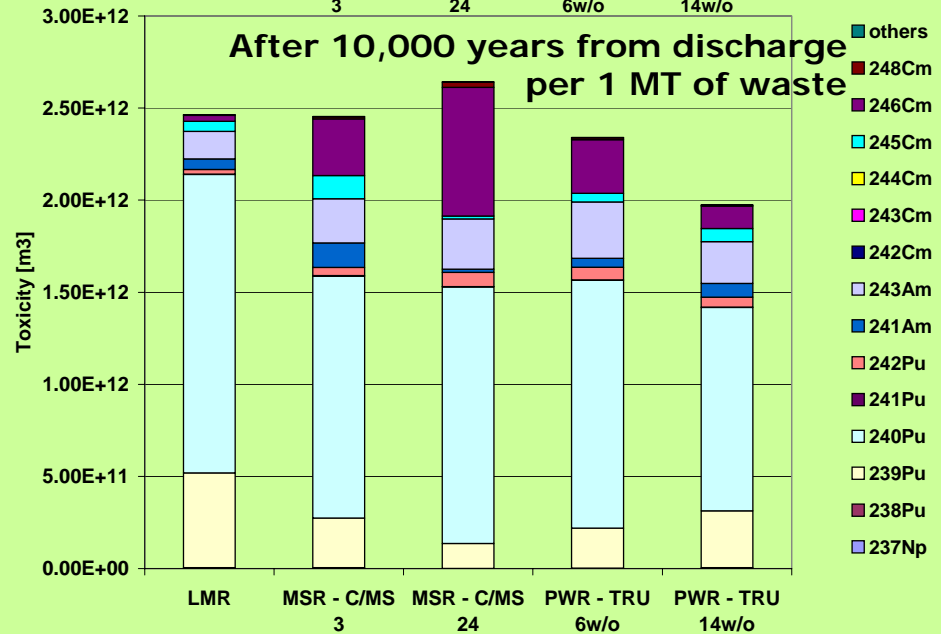
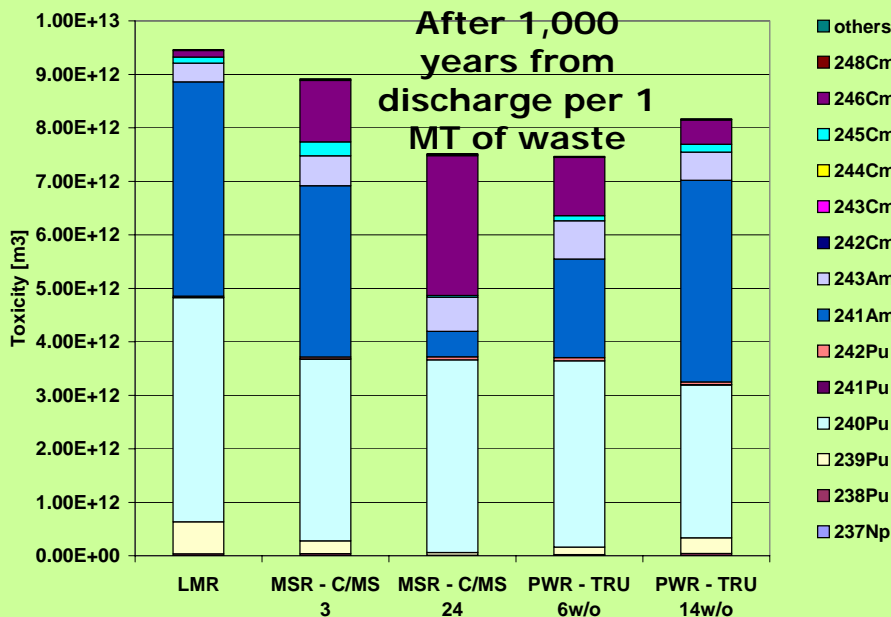
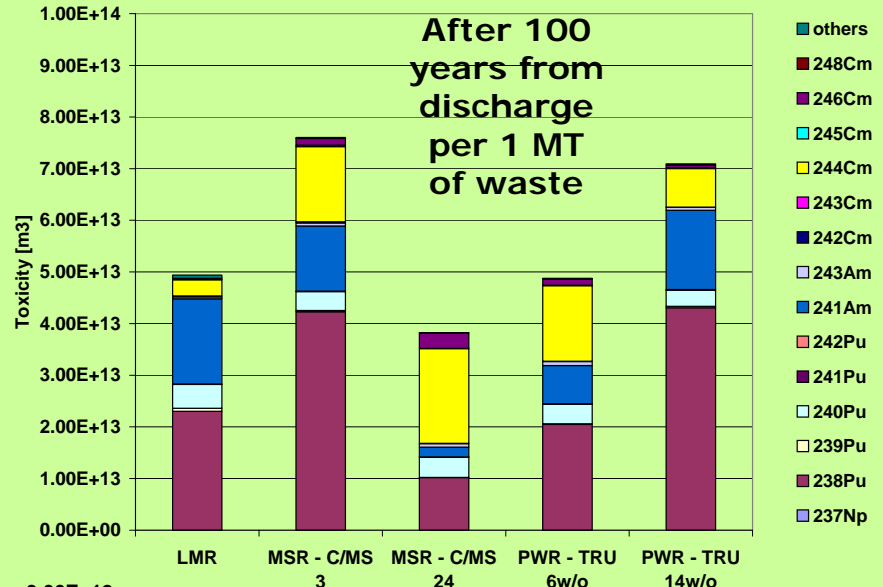
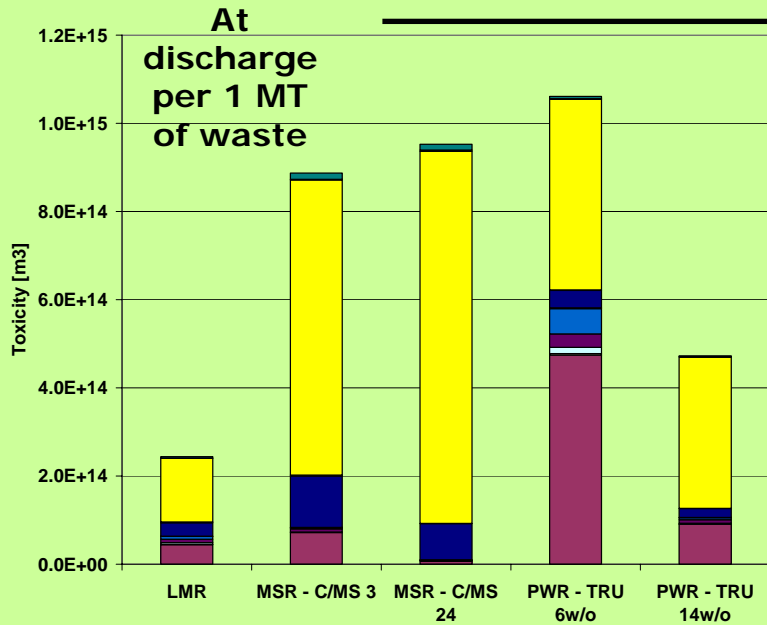
4. Fractional Transmutation



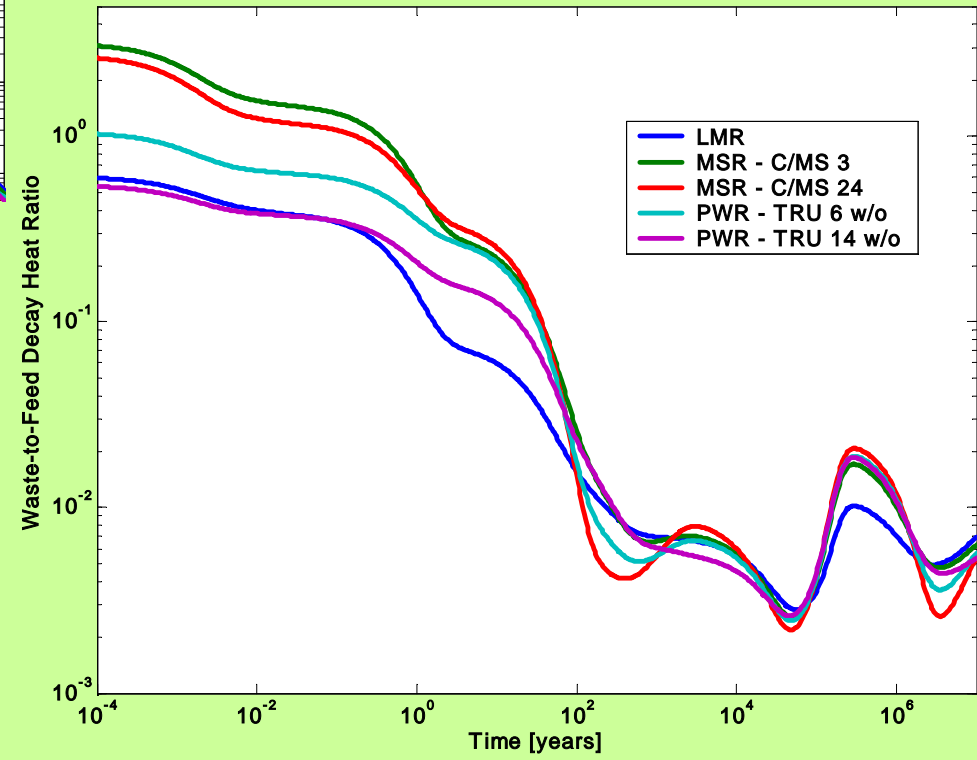
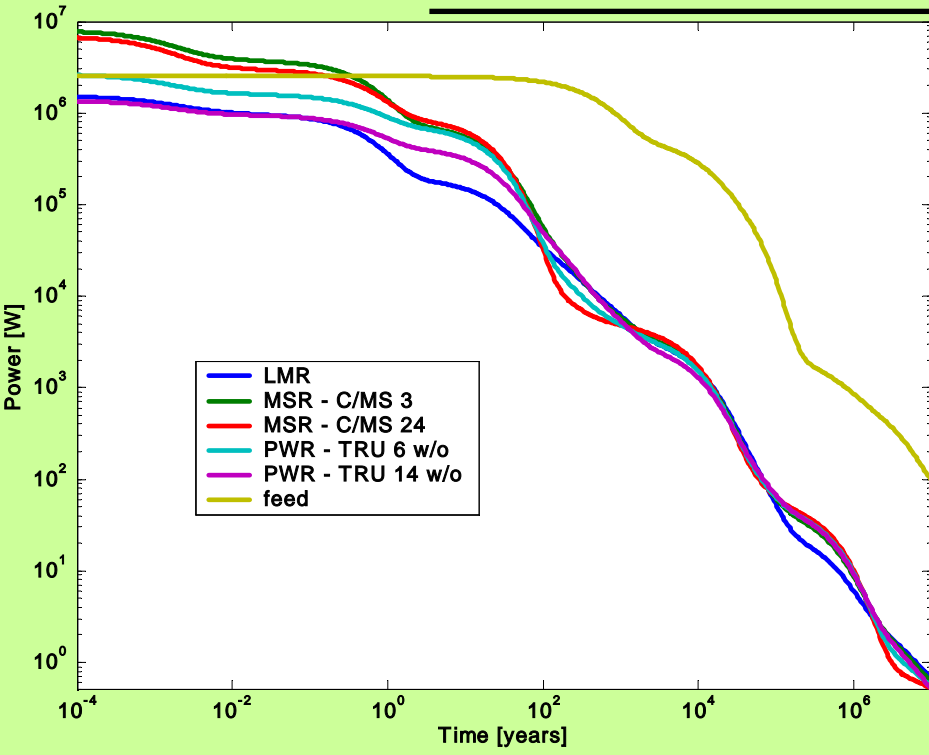
4. Toxicity



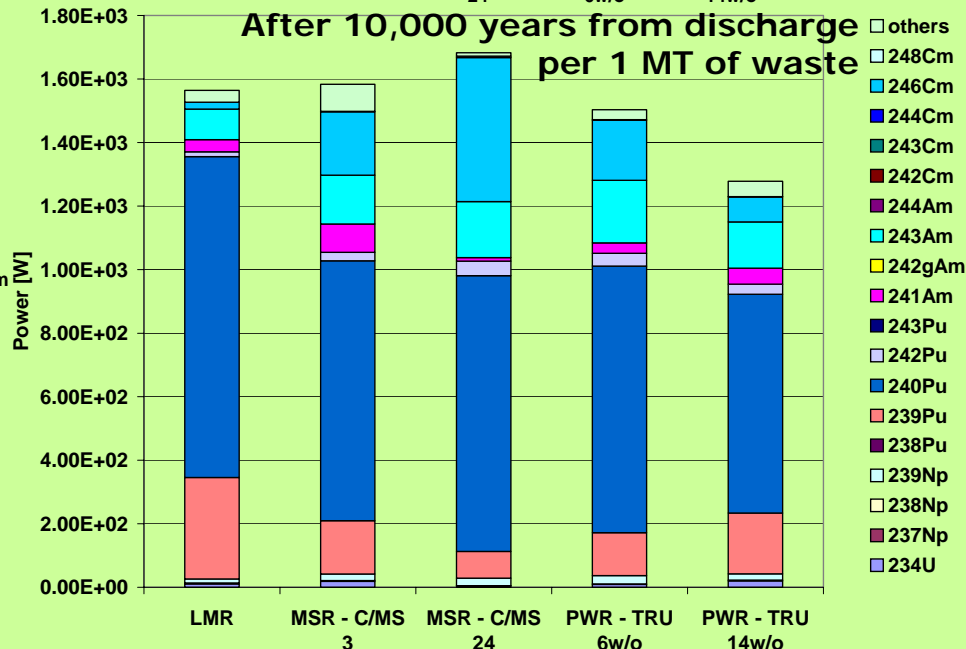
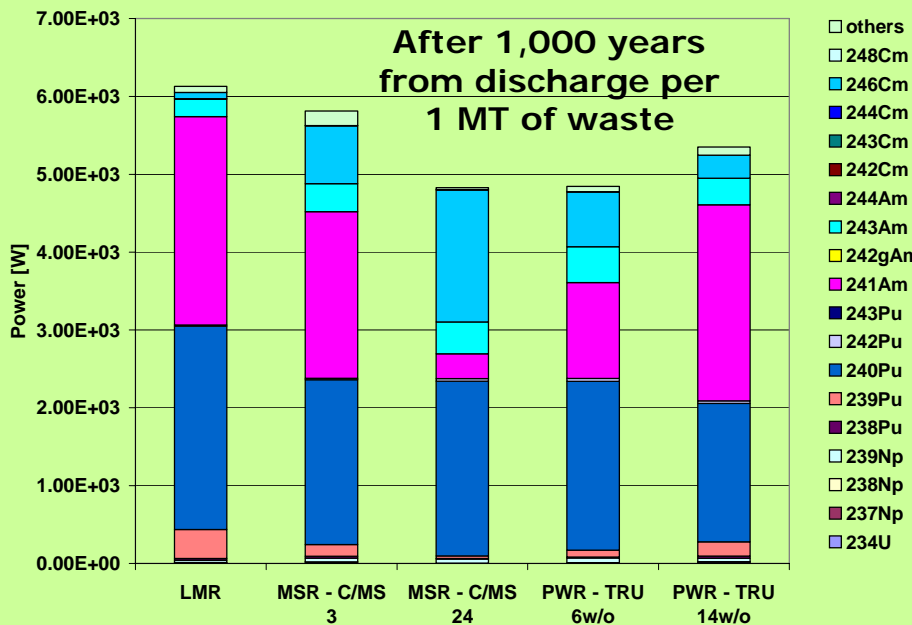
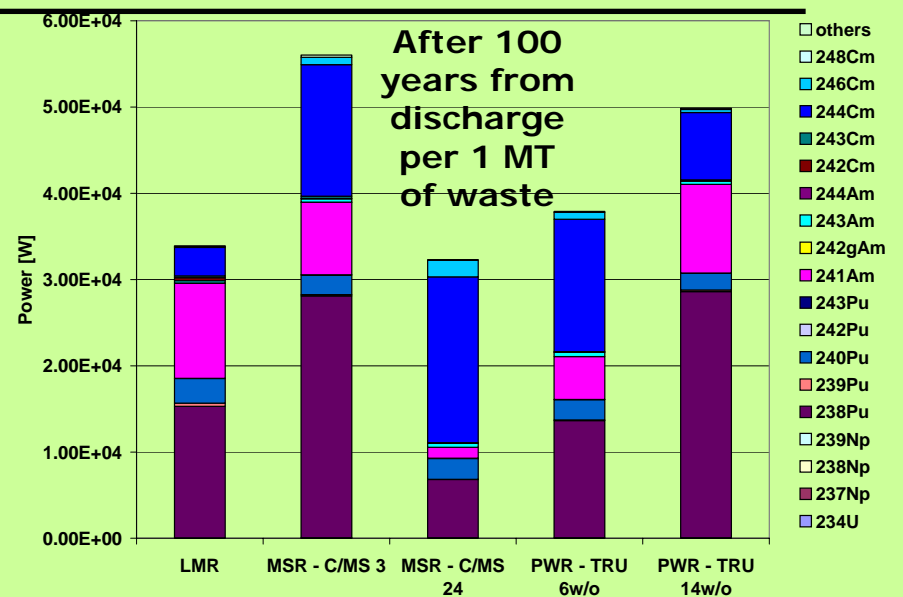
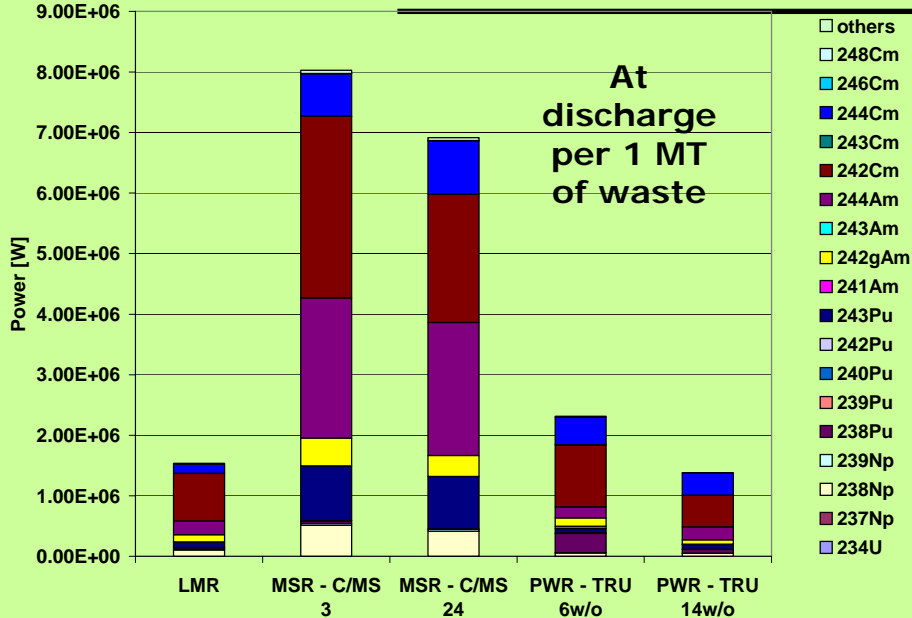
4. Toxicity



4. Decay Heat



4. Decay Heat

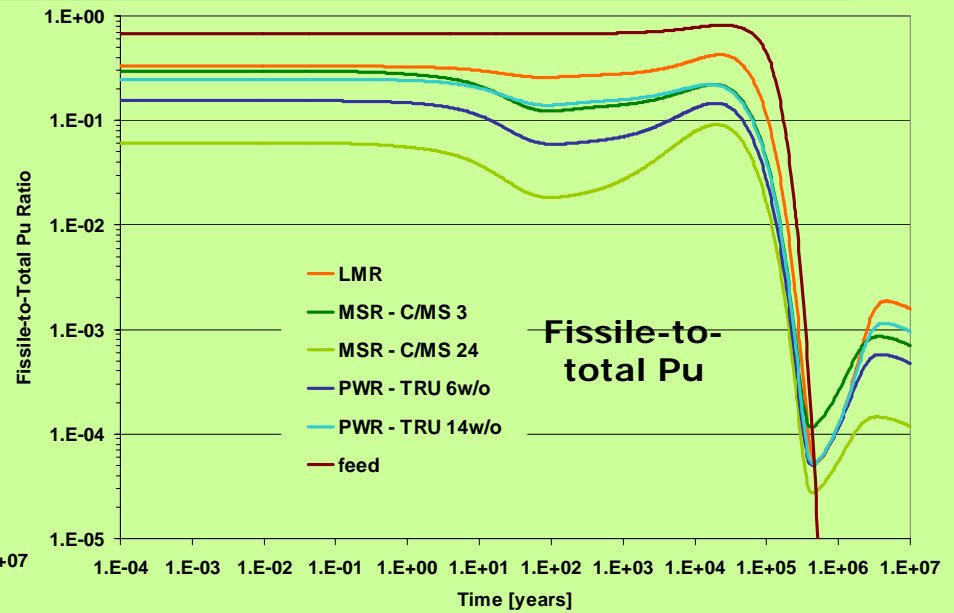
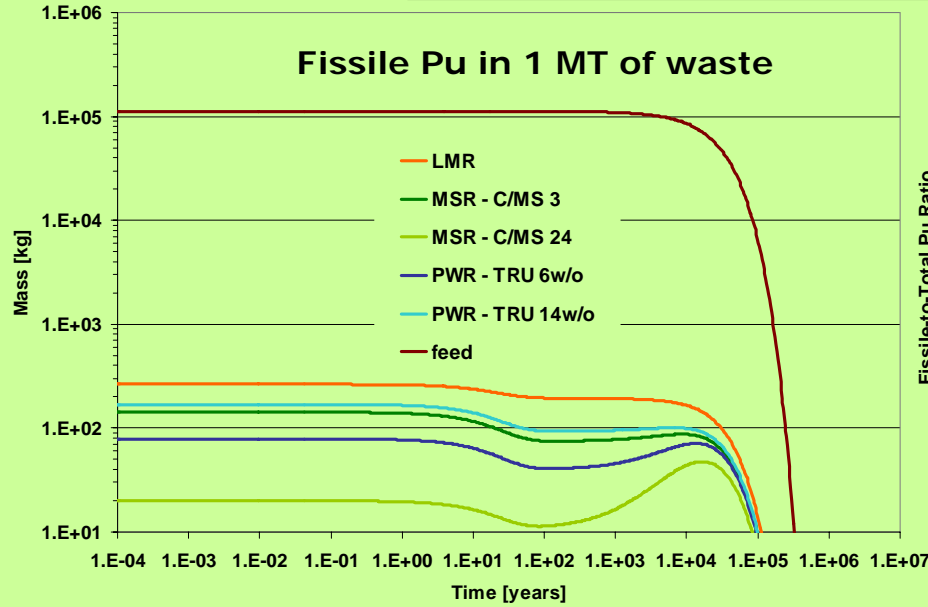


4. Np Inventory

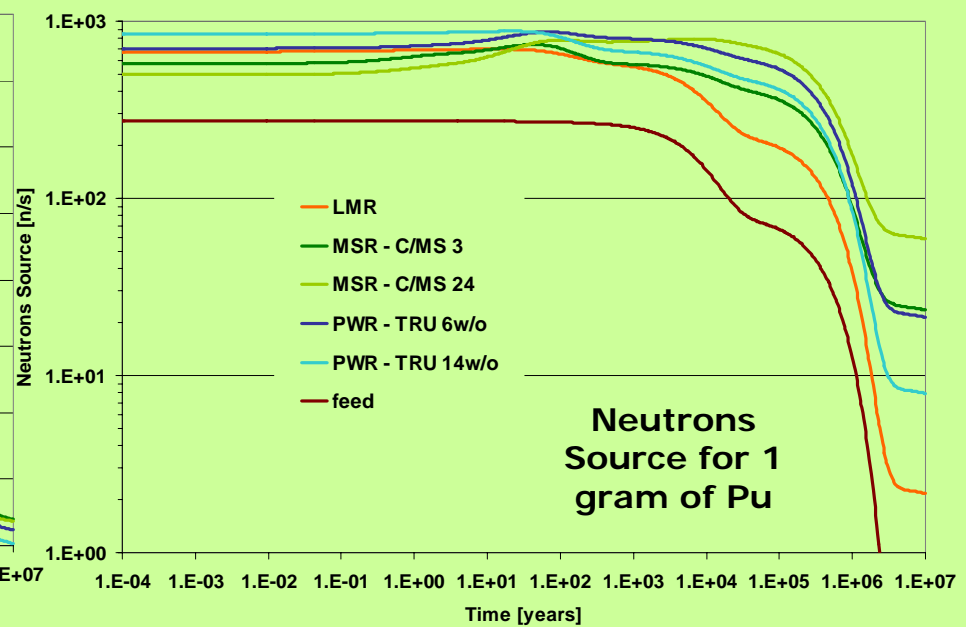
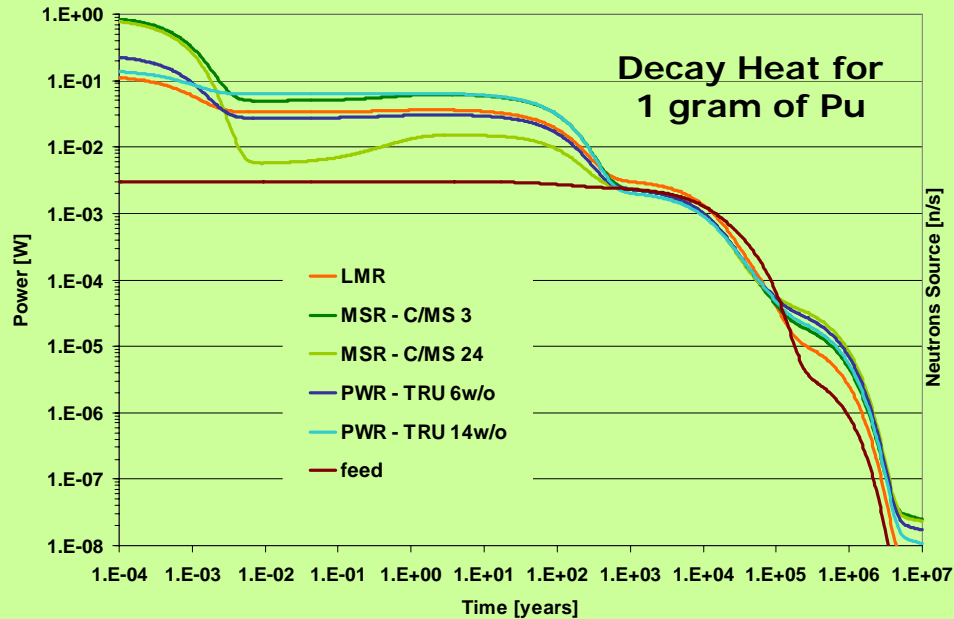
Actinide	LMR	MSR C/MS 3	MSR C/MS 24	PWR TRU 6 w/o	PWR TRU 13 w/o	Feed
^{237}Np [kg]	19.42	21.25	8.96	18.73	18.92	10674
^{241}Pu [kg]	71.00	69.30	9.65	39.34	76.79	8051
^{241}Am [kg]	39.86	14.80	3.05	10.36	26.20	19066
^{245}Cm [kg]	14.24	32.71	4.05	12.05	18.37	19
^{249}Cf [kg]	1.35	14.52	35.30	13.38	4.99	0
Total [kg]	145.87	152.58	61.02	93.86	145.27	37810

4. Pu Inventory

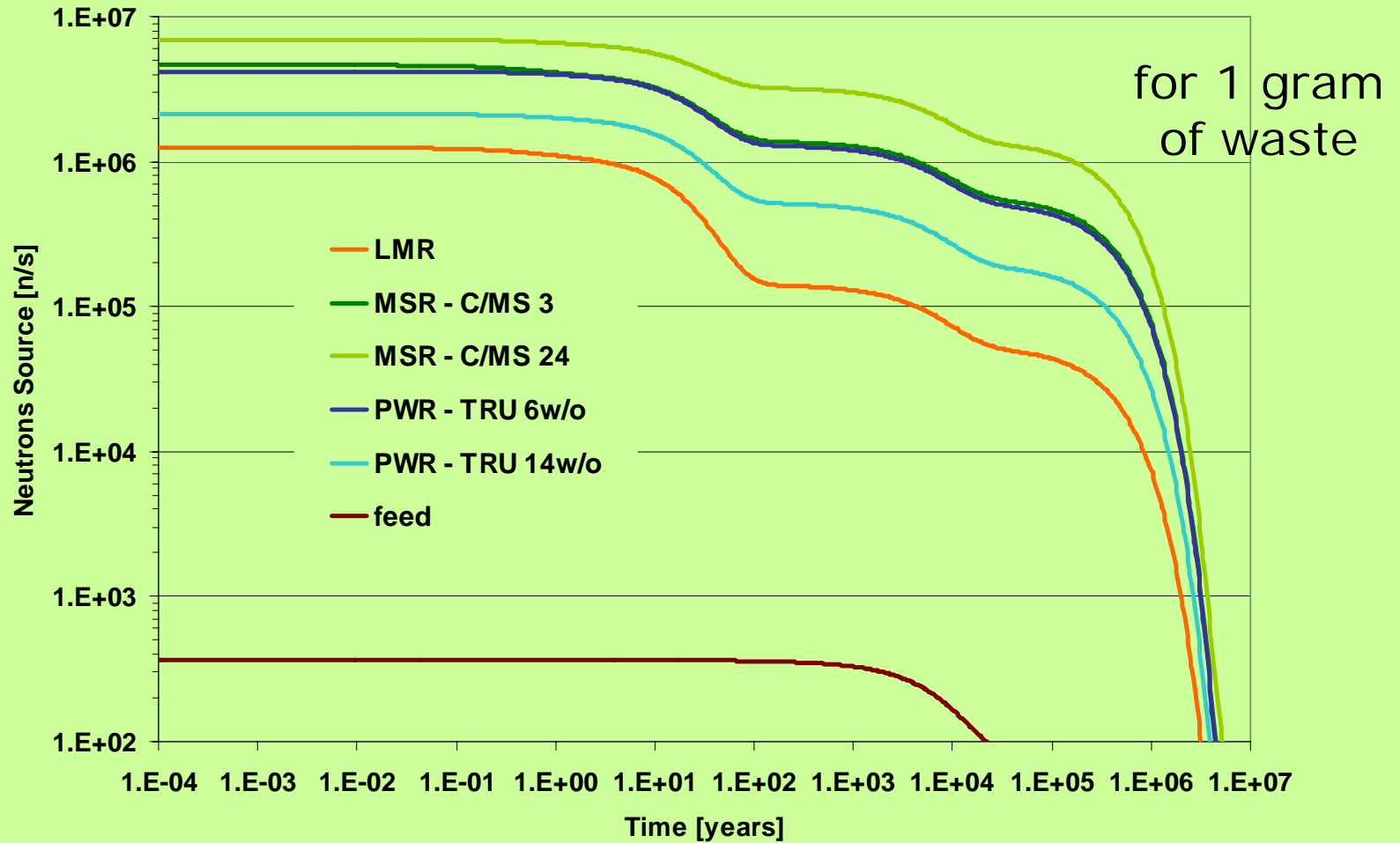
Fissile Pu in 1 MT of waste



Decay Heat for 1 gram of Pu



4. Neutrons Source



Conclusions: MSR Design

1. *It is not possible to design a NaF-ZrF₄ MSR fed by LWR SF TRU to be critical, but very close to critical – $k_{eff} \sim 0.97$, provided fission products are continuously extracted*
2. *Maximum k_{eff} is obtained when $C/MS = 3.2$*
3. *Using graphite reflectors it is possible to make the radiation damage to graphite very uniform*
4. *Decreasing the MS feed rate increases the transmutation efficiency without significantly affecting k_{eff} , provided fission products are continuously extracted*
5. *Power density reduction enhances the graphite lifetime but strongly decreasing k_{eff}*
6. *Softer spectrum is better for reducing long term inventory of ²³⁷Np, fissile Pu and Pu(fissile)/Pu ratio*
7. *Hard spectrum is better for reducing initial radio-toxicity and decay heat but after ~100 years of cooling softer spectrum is preferable*

Conclusions: Comparison

Characteristic	Preferred System
Neutron economy	LMR, PWR(14), MSR(3)
Specific power	MSR
Radio-toxicity	LMR < 10 ² y; MSR(24) < 10 ³ y; LWR(14) < 10 ⁵ y
Decay-heat	LMR < 10 ² y; MSR(24) < 10 ³ y; LWR(14) < 10 ⁵ y
Neutron source (low)	LMR, PWR(14), MSR(3)
²³⁷ Np & precursors	MSR(24), LWR(6), rest
Fissile Pu	MSR(24), LWR(6), MSR(3)
Fissile/total Pu	MSR(24), LWR(6), MSR(3)
Specific Pu decay heat (low)	MSR(24), LWR(6), LMR
Specific Pu neutron source	MSR(24), MSR(3) < 10 y; LMR, MSR(3) > 10 y

Discussion

Issues to be considered:

- *Feasibility of criticality using other MS*
- *Graphite replacement strategy*
- *TRU losses during recycling of C & FP*
- *Handling of fission products*
- *Approach to equilibrium*
- *Economics*
- *Technology maturity*